INVESTIGATION OF DYNAMIC BEHAVIOR OF POWER SYSTEM INSTALLED WITH STATCOM

BY

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In
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DEANSHIP OF GRADUATE STUDIES

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12/11/2012
Date
Dedicated

to

My Beloved Grand Mother, Aba, Maa

and

Brothers, Sisters
Acknowledgements

In the name of Allah, Most Gracious, Most Merciful. Read! In the name of your Lord and Cherisher, Who has Created (all that exists). He has created man from a clot (a piece of thick coagulated blood). Read! And your Lord is the Most Generous. Who has taught (the writing) by the pen. Taught man that which he knew not. Nay! Verily, man does transgress (in disbelief and evil deed). Because he considers himself self-sufficient. Surely, unto your Lord is the return.

(Surah 96. Al-'Alaq. The Holy Quran)

All praise be to Allah the Lord of the worlds, for having guided me at every stage of my life. I seek His mercy, favor and forgiveness. I feel privileged to glorify His name in the sincerest way through this small accomplishment.

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Nomenclature

English Symbols

\[X\] Transmission line reactance
\[H\] Inertia constant
\[M\] Inertia coefficient, \(M = 2H\)
\[D\] Damping coefficient
\[K_p, K_d, K_i\] Gains of PID controller
\[\text{p.u.}\] Per unit quantities
\[\text{pf}\] Power factor
\[P_e\] Electrical power output from the machine
\[eq\] Internal voltage across \(x_q\)
\[V_t\] Machine terminal voltage
\[P_m\] Mechanical power output to the machine
Greek Symbols

\( \psi \)  Phase angle of the mid-bus voltage  
\( e'_q \)  Internal voltage on q-axis proportional to field flux linkage  
\( E_{fd} \)  Generator field voltage  
\( \delta \)  Angle between q-axis and the infinite busbar  
\( T'_{do} \)  Open-circuit field time constant  
\( K'_A \)  Exciter gain  
\( T'_A \)  Exciter time constant  
\( x_q \)  Quadrature axis reactance  
\( x_d \)  Direct axis reactance  
\( x'_d \)  Direct axis transient reactance  
\( w_o \)  Radian frequency  
\( i_d, i_q \)  Armature current, direct and quadrature axis components  
\( v_d, v_q \)  Armature voltage, direct and quadrature axis components  
\( V_b \)  Infinite busbar voltage  
\( V_m \)  STATCOM bus voltage or mid-bus voltage  
\( \dot{g} \)  Derivative of \( g \)

Abbreviations

AC  Alternating current  
DC  Direct current
<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>FACTS</td>
<td>Flexible AC transmission system</td>
</tr>
<tr>
<td>SVC</td>
<td>Static Var compensor</td>
</tr>
<tr>
<td>TCSC</td>
<td>Thyristor controlled series capacitor</td>
</tr>
<tr>
<td>TCPAR</td>
<td>Thyristor controlled phase angle regulator</td>
</tr>
<tr>
<td>STATCOM</td>
<td>Static synchronous compensator</td>
</tr>
<tr>
<td>STATCON</td>
<td>Static condensor</td>
</tr>
<tr>
<td>SSSC</td>
<td>Static synchronous series compensator</td>
</tr>
<tr>
<td>UPFC</td>
<td>Unified power flow controller</td>
</tr>
<tr>
<td>PID</td>
<td>Proportional-integral-derivative</td>
</tr>
<tr>
<td>PWM</td>
<td>Pulse width modulation</td>
</tr>
<tr>
<td>PSS</td>
<td>Power system stabilizer</td>
</tr>
<tr>
<td>GTO</td>
<td>Gate turn-off thyristor</td>
</tr>
<tr>
<td>IGBT</td>
<td>Insulated Gate bipolar transistor</td>
</tr>
<tr>
<td>MTO</td>
<td>Metal-oxide semiconductor turn-off thyristor</td>
</tr>
<tr>
<td>IGCT</td>
<td>Insulated Gate commutated thyristor</td>
</tr>
<tr>
<td>VSC</td>
<td>Voltage-sourced converter</td>
</tr>
<tr>
<td>SMIB</td>
<td>Single-machine infinite-bus</td>
</tr>
</tbody>
</table>
THESIS ABSTRACT

Name: Muhammad Fareed Kandlawala

Title: Investigation of Dynamic Behavior of Power System Installed With STATCOM

Degree: Master of science

Major Field: Electrical Engineering

Date of Degree: December 2001

A Static synchronous compensator (STATCOM) is one of the new generation flexible AC transmission system (FACTS) devices with a promising feature of applications in power system. STATCOMs are used to stabilize the system by exchanging reactive power with the power system. In this thesis, dynamic behavior of the single machine infinite bus power system with STATCOM has been investigated. Both an approximate and a detailed mathematical model are used for damping control of a power system. The effect of PID controllers in damping enhancement has been investigated. It was observed that proportional and derivative control is superior to other combinations of PID. The simultaneous control of electromechanical transient damping and STATCOM voltage variation was found to be difficult. A robust STATCOM controller design is presented. Method of multiplicative uncertainty has been employed to model the variations of the operating points in the system. The design is carried out applying robustness criteria for stability and performance. A loop-shaping technique has been employed to select a suitable open-loop transfer function, from which the robust controller is constructed. The proposed controller has been tested through a number of disturbances including three-phase faults. The robust controller designed has been demonstrated to provide extremely good damping characteristics over a good range of operating conditions.

Keywords: Power System, FACTS, STATCOM, Loop-shaping method, $H_{\infty}$ Control, PID Controller, Robust Controller

Master of Science Degree

King Fahd University of Petroleum & Minerals, Dhahran.
December 2001
خلاصة الرسالة

الاسم: محمد فريد كايند لاولا
العنوان: بحث السلوك النشط لسائط طاقة زركب مع Statcom
الماجستير في العلوم
الدرجة: الهندسة الكهربائية
التخصص الرئيسي: كهروماجستير
تاريخ التخرج: كانون أول "ديسمبر" 2001

بعد المعادل المتزامن الثابت (FACT) أحد أنظمة الجيل الجديد في إرسال الطاقة المتزامن STATCOM يشير FACT إلى أن المعادل المتزامن الثابت STATCOM يتم استخدامه في بيئة تابعة للطاقة المتزامنة. إنه نظام طاقة متكامل أحادي ذات ناقل لا متناهي. تم استخدام المعادل المتزامن الثابت (FACT) في تحسين التواصل PID وآخر تقنيات التحكم في المتزامنة لنظام الطاقة. تم بعد أن مضليات PID والتناسب كانت أفضل من باقي إعدادات PID الأخرى. وجد أن مضليات PID من STATCOM هي عملية صعبة. تم تكوين تصميم مضليت ذات ثبات قوي من STATCOM وتعويضات الفولتية لFACTS. التحكم في نقطة التشغيل في النظام، تم استخدام تكنولوجيا استخدام معايير ثبات قوي للإحترام والأداء. تم تطبيق تقنية تشغيل العقد لإنتاج دارة النقل المناسبة و التي تم من خلالها بناء مضليت ذات ثبات عالي. تم عرض كيفية استخدام هذا المضليت ذو الثبات العالي لإعطاء ميزات مضللة جيدة جداً على تشغيل هاوسة من ظروف التشغيل.

PID, STATCOM, FACTS, طرق تشغيل العقدة, ضبط, H, مضليت ذو ثبات قوي.

الكلمات الرئيسية: نظام طاقة،

درجة الماجستير في العلوم
جامعة الملك فهد للتربة والمعادن
كانون أول "ديسمبر" 2001
Chapter 1

Introduction

1.1 Introduction

An AC power system is a complex network of synchronous generators, transmission lines and loads. The transmission lines can be represented mostly as reactive networks composed of series inductors and shunt capacitors. The total series inductance, which is proportional to the length of the line, determines primarily the maximum transmissible power at a given voltage. The shunt capacitance influences the voltage profile and thereby the power transmission along the line.

The transmitted power over a given line is determined by the line impedance, the magnitude of, and phase angle between the end voltages, or in other words, the forcing voltage acting across the transmission line.

The basic operating requirements of an AC power system are that the synchronous generators must remain in synchronism and the voltages must be kept
close to their rated values. The capability of a power system to meet these requirements in the face of possible disturbances such as line faults, generator and line outages and load switching etc. is characterized by its transient, dynamic and voltage stability. The stability requirements usually determine the maximum transmittable power at a stipulated system security level.

Since the 1970s, energy cost, environmental restrictions, right-of-way difficulties together with other legislative, social and cost problems have delayed the construction of both generations facilities, and in particular, new transmission lines. In this time period, there have also been profound changes in the industrial structure, often with significant geographic shifts of highly populated areas. In the last few years, there has been a worldwide movement of deregulation, which, in order to facilitate the development of competitive electric energy markets, stipulates "unbundling" the power generation from transmission and mandates open access to transmission services [1].

The economic, social, and legislative developments had fueled the review of traditional power transmission theory, and the creation of new concepts that allow full utilization of existing power generation and transmission facilities without compromising system availability and security.

In the late 1980s, the Electric Power Research Institute (EPRI) in the USA formulated the vision of the Flexible AC Transmission System (FACTS) in which various power electronics based controllers regulate power flow and transmission voltage and, through rapid control action, mitigate dynamic disturbances[1].
N.G.Hingorani [2, 3, 4, 5] proposed the concept of FACTS devices that involves the applications of high power electronic controllers in AC transmission networks that enable fast and reliable control of power flows and voltages.

FACTS technology is not a single high power controller but rather a collection of controllers that can be applied individually or collectively to control the interrelated parameters. The main objectives of FACTS are:

- Regulation of power flows in prescribed transmission routes.

- Secure loading of lines near their thermal limits.

- Prevention of cascading outages by contributing to emergency control.

- Damping of oscillations which can threaten security or limit the usable line capacity and improve system stability in general.

Table 1.1 shows that the FACTS controllers can be broadly classified into two classes:

- Shunt connected controllers providing voltage control

- Series connected controllers providing power flow control

The simplified expression for power flow in a lossless transmission line is given by,

$$ P = \frac{V_s V_R \sin(\delta_{SR} + \phi)}{X} $$

(1.1)
<table>
<thead>
<tr>
<th>Name</th>
<th>Type</th>
<th>Main Function</th>
<th>Controller Used</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>SVC</td>
<td>Shunt</td>
<td>Voltage Control</td>
<td>Thyristor</td>
<td>Variable Impedance Device</td>
</tr>
<tr>
<td>TCSC</td>
<td>Series</td>
<td>Power Flow Control</td>
<td>Thyristor</td>
<td>Variable Impedance Device</td>
</tr>
<tr>
<td>TCPAR</td>
<td>Series and Series</td>
<td>Power Flow Control</td>
<td>Thyristor</td>
<td>Phase Control</td>
</tr>
<tr>
<td>STATCOM</td>
<td>Shunt</td>
<td>Voltage Control</td>
<td>GTO</td>
<td>Variable Voltage Source</td>
</tr>
<tr>
<td>SSSC</td>
<td>Series</td>
<td>Power Flow Control</td>
<td>GTO</td>
<td>Variable Voltage Source</td>
</tr>
<tr>
<td>UPFC</td>
<td>Shunt and Series</td>
<td>Voltage and Power Flow Control</td>
<td>GTO</td>
<td>Variable Voltage Source</td>
</tr>
</tbody>
</table>

Table 1.1: FACTS Controllers

where \( V_S \) and \( V_R \) are sending and receiving end bus voltages, \( X \) is the series reactance of the line \( \delta_{SR} \) is the phase difference in the bus angles, \( \phi \) is the phase angle shift introduced by a phase angle regulator (phase shifting transformer).

It is obvious from Eq. (1.1) that the control of voltage, series reactance and phase angle (\( \phi \)) have effect on the power flow. While the control over the voltage and series reactance can be used to increase the power limit. The control over \( \phi \) can be used to regulate power flow in the loops.

### 1.2 Static synchronous compensator (STATCOM)

The new generations of FACTS controllers are based on voltage source converter, which use turn-off devices like GTOs. These controllers require lower ratings of passive elements (inductors and capacitors) and the voltage source characteristics present several advantages over conventional variable impedance controllers.

The general arrangement of an STATCOM device is shown in Fig. 1.1. The solid-state synchronous voltage source, implemented by a voltage source converter,
Figure 1.1: The general arrangement of STATCOM.

is operated as a shunt connected static VAR compensator (SVC). This arrangement of SVC exhibits operation and performance characteristics similar to that of an ideal rotating synchronous condenser and for this reason was called Static synchronous condenser (STATCOM)[7]. Other names of the device are static synchronous compensator (STATCOM) and advanced static VAR compensator (ASVC). Recent literature uses the name STATCOM instead of STATCON.

The voltage sourced converter produces a set of three phase voltages that are in phase with the corresponding bus voltage. The reactive power is varied by varying the magnitude of the converter output voltages. A small phase difference exists in steady state, depending on reactive power output, so that real power can be drawn from the lines to compensate for the losses. The current on the DC side is mainly a ripple of magnitude much smaller than the AC line currents. As no real energy
exchange, except to compensate for the losses, takes place in steady state, the DC voltage can be maintained by a capacitor. The major advantages of the STATCOM over the SVC are [6, 7]

- The STATCOM can supply required reactive current even at low values of bus voltage, whereas the reactive current capability of SVC at its susceptance limit decreases linearly with decrease in bus voltage. The STATCOM is therefore, superior to SVC in maintaining system voltage.

- With proper choice of device ratings and thermal design, STATCOM can have a short time overload capability. This is not possible in an SVC because there is an inherent susceptance limit support.

- Significant size reduction can be achieved because of reduced number of passive component and their small size.

- STATCOM can allow for real power modulation if it has energy storage at its DC terminals.

- The ability of STATCOM to produce full capacitive output current at low system voltage also make it highly effective in improving the transient (first swing) stability.

- The transient stability margin obtained with the STATCOM is significantly greater than that attainable with the SVC of identical rating. This means that the transmittable power can be increased if the shunt compensation is
provided by the STATCOM rather than SVC, or in other words, for the same stability margin, the rating of STATCOM can be decreased below that of the SVC.

1.3 Literature Review

1.3.1 Basic concept

The technical concept of the voltage-sourced advanced static VAR generator (ASVG) employing gate turnoff (GTO) thyristors was given in an article published in 1988 [8]. The article gives an overview of the electrical and mechanical configurations of ± 100 MVAR prototype ASVG and the details of the test performed on it.

In 1994, Laszlo Gyugyi gave the basic concept of STATCOM using voltage-sourced converter [6]. In his paper, he described the basic operation of STATCOM and the functional control scheme to control the STATCOM used for both reactive and real power compensation.

Analysis of 6 and 12 pulse STATCOM is given in [8]. A study of conditions leading to circuit resonance is carried out together with possible method of avoiding such problems. Study of multilevel topologies of STATCOM has been presented in [7, 9].
1.3.2 Modeling, analysis and control design

Schauder and Mehta [10] proposed a vector control scheme for control of reactive current using STATCOM. They described two controller structures for the STATCOM one of which involves both magnitude (using PWM strategy) and phase control of inverter, and the other structure uses only phase angle control. For the latter controller structure the system is not amenable to linear output feedback control in all operating regions. Authors proposed a nonlinear state feedback controller to overcome this problem.

Design of the voltage controller and the analysis of its dynamic behavior using eigenvalue analysis and its simulation are presented in [11]. The paper concentrates on the application of STATCOM for the reactive power compensation of a long transmission line by regulating the voltage at its mid point. It has been found that the plant transfer function is of the minimum phase type. Eigenvalue analysis using linearized model was carried out to design a compensator in cascade with an integral controller to overcome this problem.

A comparative study for dynamic operation of different models of STATCOM and their performance is given in [12].

Averaged modeling and nonlinear control of advanced static VAR compensator (ASVC) was given in [13]. The generalized averaged method has been used to get time invariant continues nonlinear model of the system. It was shown that for this system a PI controller with constant parameters is not robust enough because of the
variation of the pole zero frequency with the operating point. A nonlinear controller based on linearization via feedback associated with a proportional controller has been chosen. The internal stability has been investigated and it is guaranteed on the whole STATCOM operating range.

Design of a nonlinear controller for STATCOM based on the differential algebra theory is presented in [14]. The controller designed by this method allows linearizing the compensator and controlling directly the capacitor voltage and output reactive power of the STATCOM. Such a control enables to stabilize the compensation system and thus helps to improve largely the transient performance of the global system.

Y. Ni [15] proposed a nonlinear PID controller on STATCOM with differential tracker for damping the inter-area oscillations. The simulation results showed good performance of the suggested differential tracker under large disturbances.

A rule-based controller for STATCOM was proposed in [16]. The paper analyzes the synchronizing and damping torque induced on the shaft of the generator by STATCOM in a single machine infinite bus (SMIB) system. It was found that the induced damping torque always decreases with the strengthening of the voltage control. Moreover, a fixed-parameter PI damping controller can be invalid or even provide the system with negative damping for certain system parameters and load conditions. Based on the synchronizing and damping torque coefficient calculation, a rule based controller, which employs bang-bang, fuzzy logic or fixed-parameter PI control strategy according to operation state of the system is designed to compromise the conflict between the control objectives.
Design of dynamic controller for SVC and STATCOM is the topic of very recent articles [17, 18] for steady state, transient stability and eigen value studies.

The thyristor controlled STATCOM with new double firing phase control which makes it possible to control the active and the reactive power directly and independently without any sacrifice of the harmonic characteristic is presented in [19]. The 12-pulse configuration is used for reducing the harmonics further.

In [20] the author described a technique to control the harmonic output of a STATCOM using a PWM scheme with a minimal number of additional switchings. A neural network algorithm was developed to define the switching instants. The technique seems to offer a better alternative to other conventional methods.

Fuzzy logic controllers are also used for STATCOM in interconnected system to improve the dynamic behavior of the system [21].

An optimal robust control procedure for SVC was presented in [22]. Variation of system operation conditions are represented by an unstructured uncertainty model. Structure singular value (μ) optimization together with model reduction techniques are used to design a low order controller which provides fast and stable voltage regulation under all system conditions. The effectiveness of the procedure was shown on a weak radial system with multiple SVCs. The $H_{\infty}$ controller out-performs the classical PI control.

The problem of interaction between dynamic loads and FACTS controllers has been investigated in [23]. Authors show that while an accurate modeling of loads in power system is a difficult task and often uncertain because of the non-deterministic
characteristic of the loads, but proper FACTS regulations can improve the overall robustness of the system. Two methods have been presented, one based on eigenvalue sensitivity and residue technique, which takes into account the uncertain characteristics of dynamic load to compute the most efficient phase compensation for low frequency oscillation damping. The second approach is based on designing a robust controller by linear matrix inequalities techniques for guaranteeing a certain degree of stability and performance of the FACTS controller.

A Supplementary control of SVC and STATCOM using $H_\infty$ control is proposed for improving the damping of synchronous machines oscillations in [24]. The power system considered for the simulation was a 2-generator 4-bus system. The dynamic response of the synchronous machines subjected to a three-phase fault are given to demonstrate the effectiveness of the supplementary control of SVC and STATCOM. Results indicate both SVC and STATCOM can provide smoother voltage profiles as well as better damping characteristic under disturbance conditions.

A robust nonlinear controller is proposed for STATCOM voltage control in [25]. Direct feedback linearization technique was employed to transform the nonlinear model into a linear one. The Riccati equation approach is then used to design the robust controller for the linearized model. Simulation studies show that in addition to the true system parameters, the bounds of the plant unknown time-varying parameters are also needed for the design, and the overall system was found to be asymptotically stable for all admissible uncertainties.

In [26], author pointed out that the mid-point location, which was described
as the best location for the SVC, is also a possible best location of the modern FACTS devices such as STATCOM for voltage support. For the system considered, he showed that it doubled the power transfer of the line and facilitated independent control of the reactive power at both ends of the transmission line.

1.3.3 Application of STATCOM for stability improvement

In [27], authors demonstrated that a distributed STATCON (D-STATCON), applied in a distribution system, could be either used to greatly increase the load or distance served by the voltage-limited lines compared with existing conventional means. Use of D-STATCOM appears to be particularly advantageous for lumped loads, where its rapid response and broad voltage control capacity can be fully exercised.

The use of FACTS controller generates significant harmonics in the power system. These harmonics can be eliminated by the multiple inverter connection and the use of zig-zag transformers [28]. The paper outlines the experimental arrangements and early results for a 24-pulse STATCOM.

A comparative study between the conventional SVC and STATCOM for effectiveness in damping power oscillations is given in [29]. Comparative study of two damping controllers, power system stabilizers (PSS) and STATCOM for damping enhancement of generator oscillations occurring in a system subject to disturbances by employing PID controller was presented in [30, 31]. The simulation results show that proposed STATCOM controller renders better damping performance over the PSS and SVC.
In references [32, 33], authors investigated the application of STATCOM for dynamic stability of the third nuclear power plant in Taiwan power system. Simulation and analytical results show the effectiveness of the designed damping controller in terms of dynamic stability enhancement and power flow increment.

A comprehensive study was undertaken to investigate how STATCOM could be used with fixed-speed wind turbines, which use induction generator to improve both steady state and dynamic impact of a wind farm on the network[34]. An optimal power flow model based on loss minimization was developed. The simulation results show the improvement of steady state stability limit, prevention of damaging overvoltages and mitigation of the voltage fluctuations at blade passing frequency, which may occur if the rotor of a number of wind turbines fall into synchronism.

From the above cited literature, it is clear that a good amount of work have been done on different aspects of design, control and application of SVC and STATCOM for power system damping and oscillation enhancements. However STATCOM are relatively new power applications and not all aspects of their dynamic performance are fully explored.

1.4 Objectives and scope of the thesis

The application of FACTS controllers creates new challenges for power engineers, not only in hardware implementation, but also in design of control systems, planning and analysis. In particular the effectiveness of these controllers will depends
on the development of adequate and dependable control strategies. Due to the fast response of such controllers, study of a wide spectrum of transient behaviour, including network dynamics, generator rotor low frequency oscillations and torsional oscillations, etc. are necessary.

Motivated by these observations, the objective of this thesis are

- Dynamic modeling and analysis of STATCOM for a single-machine infinite-bus power system.

- Evaluation of existing control design techniques for STATCOM devices. Study the applicability of PID (proportional-integral-derivative) type in dynamic performance enhancement.

- Design of STATCOM controller which will be dependable for a good range of operating conditions (robustness of controllers) etc.

1.5 Outline of the thesis

The chapter-wise summary of the work reported is as follows.

Chapter 2 covers the basic concept of STATCOM and the mathematical modeling of the single machine infinite-bus power system installed with STATCOM. Two models have been investigated: an approximate model and a detailed model.

Chapter 3 addressed the design of various PID controllers for the approximate as well as detailed model. The simulations studies are carried out using MATLAB
and SIMULINK program.

The basic concepts of robust control, an overview of the robust stability criteria, necessary and sufficient conditions for the design of the robust controller, etc. have been presented in chapter 4. A detailed overview of the robust controller design through loop-shaping technique is also presented.

Chapter 5 presents the simulation results for both the models with the proposed robust controller.

Conclusions and suggestions for future work are presented in chapter 6.
Chapter 2

Dynamic model of a single
machine system with STATCOM

2.1 Introduction

Static synchronous compensator is a second generation FACTS device used for shunt reactive power compensation. It is based on voltage sourced converters (VSC) and used self-commutating power semiconductor devices such as GTO. Fig. 2.1 shows the basic six-pulse STATCOM. The output voltage contains substantial harmonics and therefore higher pulse numbers are usually used by combining a number of six-pulse VSCs appropriately. Alternatively, harmonics can be reduced by pulse width modulation (PWM) switching strategies. Two models of the synchronous generator connected to an infinite bus with a STATCOM at the mid bus have been presented in this chapter. These are
- A third order model for generator and current controlled STATCOM model

- A detailed 5th order model for generator and STATCOM models

Figure 2.1: Six pulse STATCOM.

2.2 Basic concepts of voltage sourced converter

The voltage sourced converter is the building block of STATCOM, Unified power flow controller (UPFC), inter line power flow controller (IPFC) and other FACTS devices. Conventionally a thyristor device has only the turn-on control, its turn-off depends on the current coming to zero according to circuit and system conditions. Devices such as the GTO, IGBT, MTO, IGCT, etc. have turn-on and turn-off capability. These devices (referred to as turn-off devices) are more expensive and have higher losses than the thyristors without turn-off capability. However, turn-off
devices enables converter concepts that can have significant overall system cost and performance advantages. Converter applicable to the FACTS Controllers would be of the self-commutating type. There are two basic categories of self-commutating converters [35]:

- Current-sourced converters in which direct current always has one polarity and power reversal takes place through reversal of the DC voltage polarity.

- Voltage-sourced converters in which DC voltage always has one polarity and power reversal takes place through reversal of the DC current polarity.

Conventional thyristor-based converters, being without turn-off capability, can only be current sourced converters, whereas turn-off device-base converters can be of either type.

For reasons of economics and performance, voltage-sources converters are often preferred over current-sourced converters for FACTS applications.

Since direct current (DC) in a voltage-sourced converter flows in either direction, the converter valves have to be bidirectional, and also, since DC voltage does not reverse, the turn-off devices need not to have reverse voltage capability. Such turn-off devices are known as asymmetric turn-off devices. Thus, a voltage-sources converter valve is made up of an asymmetric turn-off device such as GTO with a parallel diode connected in reverse as shown in Fig. 2.2. For higher power converters, provision of separate diodes is advantageous. There would be several turn-off device-diodes units in series for high voltage applications.
Figure 2.2: Valve for a voltage sourced converter.

Figure 2.3: Voltage sourced converter concept.

Fig. 2.3 shows the basic functioning of a voltage-sources converter. On the DC side, voltage is unipolar and is supported by a capacitor. This capacitor is large enough to at least handle a sustained charge/dischage current that accompanies the switching sequence of the converter valves and shifts in phase angle of the switching valves without significant change in the DC voltage. It is also shown on the DC side that the DC current flow in either direction and that it can exchange DC power with the connected system in either direction. Shown on the AC side is the generated AC voltage connected to the AC system via an inductor. Being an AC voltage source with low internal impedance, a series inductive interface with the AC system (usually
Figure 2.4: single valve operation of voltage sourced converter.

through a series inductor and /or a transformer) is essential to ensure that the DC capacitor is not discharged rapidly into a capacitive load such as a transmission line.

Basically a voltage-sourced converter which generates AC voltage from a DC voltage is, for historical reason, often referred to as an inverter, even though it has the capability to transfer power in either direction. With a voltage-sourced converter, the magnitude, the phase angle and the frequency of the output voltage can be controlled [35].

Fig. 2.4 shows a diagram of a single-valve operation, $V_d$ assumed to be constant, supported by large capacitor, with the positive polarity side connected to the anode side of the turn-off devices. When turn-off device is turned on, the positive DC terminal is connected to the AC terminal 'A' and the AC voltage would jump to $+V_d$. If the current happens to flow from $+V_d$ to A (through device), the power would flow from the DC side to AC side (inverter action). However, if the current happens
to flow from A to $+V_d$ it will flow through diode even if the device is so called turned on, and the power would flow from the AC side to the DC side (rectifier action). Thus, a valve with the combination of turn-off device and diode can handle power flow in either direction with the turn-off device with the turn-off device handling inverter action, and the diode handling rectifier action. This valve combination and its capability to act as a rectifier or as an inverter with the instantaneous current flow in positive (AC to DC side) or negative direction respectively, is basic to voltage-sourced converter concepts [35].

2.3 Mathematical models

A single-machine infinite-bus system (SMIB) with a STATCOM connected through a step-down transformer is shown in Fig. 2.5, and its equivalent circuit is shown in Fig. 2.6.

![Figure 2.5: A SMIB system with STATCOM.](image-url)
Figure 2.6: Equivalent circuit diagram of the system of Fig. 2.5

The Following assumptions have been made for building the dynamic model of the system [16]

- No detailed exciter and governor dynamics models.

- $e_q$, the voltage behind transient reactance $x'_d$, is considered to be constant.

- The mechanical power input to the system is also constant

- STATCOM is modeled as a controllable reactive current source with time delay.

- Inductive current generated by the STATCOM is assumed to be constant.

The electromechanical swing equation for the generator is broken up into

$$\dot{\delta} = \omega_0 \omega$$

$$\dot{\omega} = \frac{1}{M} [P_m - P_e - D\omega]$$  \hfill (2.1)
The dynamics of the current controller can be written as

$$I_S = \frac{1}{T} [-I_S + Ku] \quad (2.2)$$

where

$$P_e = \frac{e_q V_m}{x'_d + X_1} \sin \theta + \frac{V_m^2}{2 \left( x'_d + X_1 \right) \left( x_q + X_1 \right)} \frac{x'_d - x_q}{\sin 2\theta} \quad (2.3)$$

$$V_{md} = \frac{(X_1 + x_q) V \sin \delta + I_S X_2 \sin \theta (X_1 + x_q)}{X_1 + X_2 + x_q} \quad (2.4)$$

$$V_{mq} = \frac{(X_1 + x'_d) V \cos \delta + e_q' X_2 + I_S X_2 \cos \theta (X_1 + x'_d)}{X_1 + X_2 + x'_d} \quad (2.5)$$

$$V_m = V_{md} + jV_{mq} \quad (2.6)$$

$\delta$ is the load angle in radian, $\omega$ is relative speed, $M$ is the inertia constant in seconds, $D$ is the damping constant, $P_e$ is delivered electrical power, $I_s$, $u$, $K$ and $T$ are the output current, controller output, gain and time constant of STATCOM, respectively. $V_m$ in Eq. (2.3) is the terminal voltage of the STATCOM, $x'_d$ and $x_q$ are the direct and quadrature reactance of the generator, respectively. $X_1$ and $X_2$ are the sum of the reactance of the transformer and transmission line as shown in Fig.2.6. $\theta$ is the phase difference between quadrature axis of the generator and is written as

$$\theta = \tan^{-1} \left( \frac{V_{md}}{V_{mq}} \right) \quad (2.7)$$

where $V_{md}$ and $V_{mq}$ are the direct and quadrature axis components of $V_m$, respec-
tively. By linearizing equations (2.1-2.7) around an equilibrium point, one gets

\[ \Delta V_m = K_{V_m}\delta \Delta \delta + K_{V_m}I_s \Delta I_s \]  
(2.8)

\[ \Delta P_e = K_{P_e}\delta \Delta \delta + K_{P_e}I_s \Delta I_s \]  
(2.9)

here,

\[ K_{V_m}\delta = \frac{\partial V_m}{\partial \delta} \]  
(2.10)

\[ K_{V_m}I_s = \frac{\partial V_m}{\partial I_s} \]  
(2.11)

\[ K_{P_e}\delta = \frac{\partial P_e}{\partial \delta} \]  
(2.12)

\[ K_{P_e}I_s = \frac{\partial P_e}{\partial I_s} \]  
(2.13)

The STATCOM current controller output is expressed as

\[ \Delta u = -C_u \Delta V_m + C_\omega \Delta \omega \]  
(2.14)

where, \( C_u \) and \( C_\omega \) are the control transfer functions in the voltage and damping control loop respectively. The entire linearized system can be described by the block diagram shown in Fig. 2.7. Detailed derivation of the system of equations is given in appendix A.

The remote signal \( \Delta \omega \) is not readily available to STATCOM, however, it can be synthesized by locally measurable variables such as terminal voltage of the STATCOM and current through transmission lines[36].
2.4 Detailed Model of the Power System With STATCOM Controller

In the detailed model of the power system with STATCOM, in addition to the swing equation of the generator, the field and excitation system dynamics are considered. The STATCOM is modeled as a voltage sourced converter behind a step down
transformer. Fig. 2.8 shows a SMIB power system installed with STATCOM which consists of a step down transformer (SDT) with a leakage reactance $X_{SDT}$, a three-phase GTO-based voltage sources converter (VSC) and a DC-capacitor. The VSC generates a controllable AC-voltage source $v_o(t) = V_o \sin(\omega t - \psi)$ behind the leakage reactance. The voltage difference between the STATCOM-bus AC voltage $V_L$ and $V_o$ produces active and reactive power exchange between the STATCOM and the power system, which can be controlled by adjusting the magnitude $V_o$ and the phase $\psi$. The voltage current relationship in the STATCOM are expressed as [37],

![Diagram](image)

Figure 2.8: STATCOM installed in a single machine infinite bus power system.
\[ I_{Lo} = I_{Lo\text{d}} + jI_{Lo\text{q}} \]
\[ V_o = cV_{DC}(\cos \psi + j \sin \psi) = cV_{DC} \angle \psi \]
\[ \frac{dV_{DC}}{dt} = \frac{I_{DC}}{C_{DC}} = \frac{c}{C_{DC}} (I_{Lo\text{d}} \cos \psi + I_{Lo\text{q}} \sin \psi) \] (2.15)

where, for the PWM inverter,

\[ c = mk; \]
\[ k = \frac{\text{AC Voltage}}{\text{DC Voltage}}; \]
\[ m = \text{modulation ratio defined by PWM}; \]
\[ \psi = \text{phase angle, defined by PWM} \]

From Eq. (2.15), it can be seen that the magnitude of the STATCOM voltage \( V_{DC} \) depends on \( c \), hence \( c \) is termed as magnitude control of the STATCOM. The complete derivation for the dynamic model of SMIB with STATCOM is given in Appendix A.

The nonlinear model of the power system of Fig. 2.8 is given as:

\[ \dot{\delta} = \omega \delta \omega \]
\[ \dot{\omega} = \frac{1}{M} [P_m - P_e - D_\omega] \]
\[ eq' = \frac{1}{T_{do'}} [E_{fd} - eq' - (x_d - x_d')I_{td}] \] (2.16)
\[ \dot{E}_{fd} = -\frac{1}{T_A} (E_{fd} - E_{fd0}) + \frac{K_A}{T_A} (V_{to} - V_t) \]
\[ \dot{V}_{dc} = \frac{c}{C_{DC}} [I_{lo\text{d}} \cos \psi + I_{lo\text{q}} \sin \psi] \]
where,

\[
\begin{align*}
P_e &= v_d I_{ld} + v_q I_{Lq} = eq'I_{Ld} + (x_d - x_d')I_{Ld}I_{Lq} \\
V_t &= \sqrt{v_d^2 + v_q^2} = \sqrt{(eq' - x_d'I_{Ld})^2 + x_q'I_{Lq}^2} \\
I_{Ld} &= \left(1 + \frac{XLB}{X_{SDT}}\right) eq' - \frac{XLB}{X_{SDT}} cV_{DC} \sin \psi - V_B \cos \delta \\
I_{Lq} &= \frac{XLB \ cV_{DC} \cos \psi + V_B \sin \delta}{X_{IL} + XLB + \frac{XL}{X_{SDT}} \left(1 + \frac{XLB}{X_{SDT}}\right) x_d} \\
\bar{I}_{lo} &= \frac{eq'}{X_{SDT}} - \frac{(x_d' + XL) I_{Lq}}{X_{SDT}} - \frac{cV_{DC} \sin \psi}{X_{SDT}} \\
\bar{I}_{lq} &= \frac{cV_{DC} \cos \psi}{X_{SDT}} - \frac{(x_q' + XL) I_{Lq}}{X_{SDT}}
\end{align*}
\]

By linearizing equations for \( I_{Ld}, I_{Lq}, \bar{I}_{lo}, \bar{I}_{lq} \) and then substituting in Eq. 2.16, the linearized system equation can be written as

\[
\begin{align*}
\Delta \delta &= \omega_b \Delta \omega \\
\dot{\Delta} \omega &= \frac{(-\Delta P_e - D \Delta \omega)}{M} \\
\Delta eq' &= \frac{(-\Delta eq + D \Delta E_{fd})}{T_{do}} \\
\Delta E_{fd} &= -\frac{1}{T_A} (\Delta E_{fd} - K_A \Delta V_t) \\
\Delta \dot{V}_{DC} &= \frac{1}{C_{DC}} \left[ (I_{lo} \cos \psi_0 + I_{lq}) \Delta c + c_0 (I_{lo} \sin \psi_0 + I_{lq} \cos \psi_0) \Delta \psi + c_0 (\cos \psi_0 \Delta I_{lo} + \sin \psi_0 \Delta I_{lq}) \right]
\end{align*}
\]

where,

\[
\begin{align*}
\Delta P_e &= K_1 \Delta \delta + K_1 \Delta eq' + K_{pDC} \Delta V_{DC} + K_{pc} \Delta c + K_{p\psi} \Delta \psi \\
\Delta eq &= K_4 \Delta \delta + K_3 \Delta eq' + K_{qDC} \Delta V_{DC} + K_{qc} \Delta c + K_{q\psi} \Delta \psi \\
\Delta V_t &= K_5 \Delta \delta + K_6 \Delta eq' + K_{vDC} \Delta V_{DC} + K_{vc} \Delta c + K_{ve} \Delta \psi
\end{align*}
\]
Arranging the state equations in a matrix form gives,

\[
\begin{bmatrix}
\Delta \delta \\
\dot{\Delta} \omega \\
\Delta \dot{eq}' \\
\Delta \dot{E}_{fd} \\
\Delta \dot{V}_{DC}
\end{bmatrix} = \begin{bmatrix}
0 & \omega_b & 0 & 0 & 0 \\
-\frac{k_1}{M} & -D/M & -\frac{k_2}{M} & 0 & -\frac{k_{pdc}}{M} \\
-\frac{k_A T_{do'}}{T_{do'}} & 0 & -\frac{k_{3}}{T_{do'}} & \frac{1}{T_{do'}} & -\frac{k_{qdc}}{T_{do'}} \\
-\frac{k_A k_5}{T_A} & 0 & -\frac{k_A k_6}{T_A} & -\frac{1}{T_A} & -\frac{k_A K_{vDC}}{T_A} \\
K_7 & 0 & K_8 0 & K_9 & 0
\end{bmatrix} \begin{bmatrix}
\Delta \delta \\
\Delta \omega \\
\Delta eq' \\
\Delta E_{fd} \\
\Delta V_{DC}
\end{bmatrix} + \begin{bmatrix}
\Delta \psi \\
\Delta \psi
\end{bmatrix}
\]

(2.21)

Fig. 2.9 shows the block diagram for the system, here \( s \) represents the laplace transform (the derivatives) of the states. The five states are \( \Delta \delta, \Delta \omega, \Delta eq', \Delta E_{fd} \) and \( \Delta V_{DC} \). \( \Delta c \) and \( \Delta \psi \) are the control inputs. The details of the derivation of the equations (2.18 - 2.21) are given in Appendix B.
Figure 2.9: Block diagram of the linearized system installed with STATCOM.
Chapter 3

Design of PID Controller

The dynamic behaviour of the power system models installed with STATCOM, presented in chapter 2, has been investigated in this chapter for different PID controllers used.

3.1 Introduction to PID controller

A basic feedback system is given in Fig. 3.1.

![Basic Feedback System Diagram]

Figure 3.1: A basic feedback system.

The transfer function of a PID controller is

$$G_c(s) = K_p + \frac{K_f}{s} + K_ds$$  \hspace{1cm} (3.1)
where,

\[ K_p = \text{Proportional gain} \]
\[ K_I = \text{Integral gain} \]
\[ K_d = \text{Derivative gain} \]

The variable \( e \) represents the tracking error, the difference between the desired input value \( R \) and the actual output \( Y \). This error signal is fed to controller, and the output of the controller is given as

\[ u = K_pe + K_I \int e dt + K_d \frac{de}{dt} \quad (3.2) \]

The proportional controller \( K_p \) will effect the steady state error and rise time. An integral control \( K_I \) controls the transient response and the steady state error. Inclusion of \( K_d \) has the effect of including anticipation in the system and making it faster. The effect of each of controllers \( K_p, K_d \) and \( K_I \) on a closed-loop system are summarized in the table [38].

<table>
<thead>
<tr>
<th>CL Response</th>
<th>Rise Time</th>
<th>Overshoot</th>
<th>Settling Time</th>
<th>S-S Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>( K_p )</td>
<td>Decrease</td>
<td>Increase</td>
<td>Small change</td>
<td>Decrease</td>
</tr>
<tr>
<td>( K_I )</td>
<td>Decrease</td>
<td>Increase</td>
<td>Increase</td>
<td>Eliminate</td>
</tr>
<tr>
<td>( K_d )</td>
<td>Small change</td>
<td>decrease</td>
<td>decrease</td>
<td>Small change</td>
</tr>
</tbody>
</table>

Table 3.1: Characteristics of PID controller in close loop system

There is a degree of dependence of these factors on each other. In fact, changing one of these variables \( K_p, K_d \) and \( K_I \) can change the effect of the other two. For this reason, the table should only be used as a reference for choosing of \( K_p, K_d \) and \( K_I \) [38].
3.2 PID controller for Simplified STATCOM Model

The block diagram of the simplified model with PID controller in the speed and
the voltage loop is given in Fig. 3.2. Because of difficulties with simulation on
MATLAB, the derivative functions was approximated as

\[ f(s) = \frac{K_ds + a}{s + b} \]  \hspace{1cm} (3.3)

with a and b are selected as 0.1 and 1 respectively.

The dynamic behavior of the generator-STATCOM system was studied consid-
ering the following three controller configurations [39]:

- Controller in speed loop only
- Controller in voltage loop only
- Controller in combined voltage-speed loop

Different combinations of proportional, integral and derivative (PID) controls
were tried in both the speed and the voltage loops. System data is given in Appendix
C. A 100 % input torque pulse for 5ms is applied to simulate the disturbance.
The uncontrolled system response is oscillatory. The following section presents the
simulation results with the above scenarios.

3.2.1 PID control in the speed loop only

The gains of the PID controller were tuned and the effect of each of the proportional,
derivative and integral controllers in the speed loop has been studied. The voltage
Figure 3.2: Block diagram for simplified model with PID controllers.

loop has been disabled during this study by keeping it open.

The gains of the proportional controller \( K_{ps} \) was varied between 0 - 150 for the 100 \% torque pulse disturbance considered. It was observed that by increasing the value of \( K_{ps} \), the system damping improves. But the increase in damping is at the cost of bus voltage excursion. Large gains, while provide enough electro-mechanical transient damping, gives large voltage variations. Satisfactory results in
terms of system damping, the bus voltage and the controller current variations has been observed for a gain around 100.

The impact of proportional plus derivative controller was then examined by holding the gain $K_{ps}$ to 100. It was observed that a slight improvement in the damping can be obtained with PD controller for $K_{ds}$ of up to 10. Increasing the gain of further results in overshoot of the bus-voltage.

A PID controller for $K_{ps} = 100$, $K_{ds} = 10$ and variable gain $K_{I_s}$ was simulated next. It was observed that inclusion of the integral controller results in oscillatory response.

Simulation results for the 100 % torque pulse disturbance with and without PID controller are given in Figures 3.3 - 3.5. Fig. 3.3 shows the rotor angle variation of the generator for the following cases. a) without stabilizing control, b) with proportional control alone, c) with proportional-derivative (PD) control and d) with proportional-integral-derivative (PID) control. Figures 3.4 and 3.5 show the corresponding variations of the mid-bus voltage and controller current outputs. A gain of $K_{I_s}=500$ was employed in the PID control. The response with integral control is worse compared to that with PD. Comparison of the three responses indicate that PD is superior in terms of damping control. The voltage variations, however, are worsened.

This study indicated that PD control is suitable in the speed loop of the STATCOM alone for the particular system model considered.
Figure 3.3: Comparative analysis of rotor angle (speed loop only) with PID controllers.
Figure 3.4: STATCOM bus voltage corresponding to Fig. 3.3.

Figure 3.5: Controller current output corresponding to Fig. 3.3.
3.2.2 PID control in the voltage loop only

The transient response with PID controller on voltage loop alone are shown in Figures 3.6 - 3.7. Fig. 3.6 gives the variation of mid-bus voltage for 100 % input torque pulse for 5 ms. The response without any control is shown by curve a. With proportional, derivative or combinations of PD, the voltage response is completely oscillatory. However, the oscillation in voltage can eliminated by choosing large gains in the proportional or derivative block gains. For \( K_{pu} = K_{dv} = 10000 \) the response is shown by curve b. The integral control makes the response worse as shown by curve c.

The corresponding rotor angle variations of the generator are plotted in Fig. 3.7. It can be seen that even though large \( K_{pu} \) or \( K_{dv} \) can eliminate voltage fluctuations (curve b, Fig. 3.6), they, virtually, have no impact on system damping.

Though the control in the voltage loop does not provide extra system damping, the role of the voltage loop should not be underestimated. The voltage loop is an essential component of the STATCOM controller from voltage regulation view point.

3.2.3 PID control in both voltage and speed loops

The PID controllers in both speed and voltage loops were next employed to investigate the damping improvement of the linearized 3rd order model. Various combinations of proportional, integral and derivative controls were used in both the speed as well as voltage loops. It was found in section 3.2.2 that a PID control in
Figure 3.6: Comparative analysis of STATCOM bus voltage (voltage loop only) with Different PID controllers.

Figure 3.7: Rotor angle variation corresponding to Fig. 3.6.
Figure 3.8: % Angular Speed Deviation with combined voltage-speed PID control. The voltage loop does not provide extra damping. However, because of its role in the voltage regulation, a nominal value of $K_{pv} = 10$ was selected. The gains in the speed controller loop were retuned for this value of $K_{pv}$.

As in speed controller alone, $K_{ps} = 100$ was again found to provide the best damping. For $K_{ps} = 100$ and $K_{pv} = 10$, various values of $K_{ds}$ were tried. It was observed that for $K_{ds} = 10$ electromechanical damping was satisfactory, but the overshoot in STATCOM bus voltage and controller current were excessive. The generator angular speed deviation, the STATCOM bus voltage and controller currents variations
Figure 3.9: STATCOM Bus Voltage with combined voltage-speed PID control.

Figure 3.10: Controller current corresponding to Fig 3.9.
are presented in Figures 3.8 - 3.10 respectively for a 100 % input torque pulse disturbance for 5ms. In each figure, curve a represents the without controller. Response due to proportional control in the speed loop is shown by curve b and that due to PD control by curve c. It was observed that an integral control worsens the generator speed as well as STATCOM bus voltage response and the response has not been shown.

From this section, it is summarized that

a) A control in the voltage loop does not contribute to system damping.

b) A PD control in the speed loop provides a reasonable damping of electromechanical variables but the voltage variations are larger control.

c) A PD control in the speed loop and proportional control in the voltage loop provides a reasonable damping of electromechanical variables but the voltage variations are larger control in the case of combined speed-voltage system.

### 3.3 PID control with detailed model

The block diagram for the detailed model of the power system installed with the STATCOM is given in Fig. 3.11. The block diagrams for the phase angle and the magnitude control circuits are given in Figures 3.13 and 3.12. The following three PID controller configurations were examined,

- Controller in the phase angle control loop
- Controller in the voltage magnitude control loop
• Controller in both voltage and phase angle control loop

![Block diagram of the linearized power system with STATCOM.](image)

Figure 3.11: Block diagram of the linearized power system with STATCOM.

![Phase control circuit block diagram.](image)

Figure 3.12: The phase control circuit block diagram.

In Figures 3.13 and 3.12, the functions $G_{\psi i}$ and $G_c$ are considered to be the PID control functions. The system is simulated for a disturbance of 100% torque pulse of 5 ms duration.
3.3.1 PID control in the phase angle control loop

Different combinations of PID control in the phase angle control loop were attempted. It was observed that none of the P, PD, or PI control is effective in providing damping. The presence of these controllers even worsen the responses. Fig. 3.14 shows the rotor angle variation when proportional or proportional plus integral controllers were used in phase angle control loop. Here, curve a represent the response without STATCOM control, curve b gives the response with proportional control and curve c with PI control. The phase angle control in the detailed representation is similar to the voltage control in the approximate model. Though the phase controller does not play any part in providing damping, it is essential for voltage regulation. In the subsequent analysis the phase control has been set to a nominal value, and the only control discussed is the magnitude control.
Figure 3.14: % Rotor angle (for phase angle control loop only) with different controllers.

3.3.2 PID control in the voltage magnitude loop for nominal phase angle control

For a nominal value of phase angle control if 1, different combinations of the PID controls in the magnitude control loop were investigated for the detailed model. Simulations carried out with the phase angle loop opened showed that PID controller in the voltage magnitude loop alone results in unstable system conditions.

For the 100 % torque pulse disturbance considered, the gains of the propor-
tional controller \((K_p)\) were varied between 0 - 30. It was observed that at very large gains the electromechanical damping improves but the STATCOM bus voltage excursions worsen. A reasonable damping of electromechanical and electrical transients is achieved for \(K_p\) of around 20.

It was observed that low \(K_I\) does not help in improving the damping. However some gain in damping is achieved for \(K_I > 100\) at the cost of overshoot in the STATCOM bus voltage.

Simulation results for the 100 % torque pulse disturbance with and without PID controller are given in Figures 3.15 - 3.16. Fig. 3.15 shows the rotor angle variation of the generator for the following cases. a) with proportional control, b) with PD control, c) with PI control and d) with PID control. Fig. 3.16 shows the corresponding variations of the mid-bus voltage.

The study of the detailed model indicates that suitably designed PID controller can enhance electromechanical damping of the system. However, variations in the electrical transients such as STATCOM bus voltage, controller current output etc. may not be acceptable.
Figure 3.15: Comparative analysis of rotor angle with different gains of PID controller.

Figure 3.16: Bus voltage corresponding to Fig. 3.15.
Chapter 4

Introduction to Robust control
and Loop-Shaping Technique

4.1 Introduction

Some of the STATCOM controllers presented in the previous chapter were observed to provide good damping properties. However, the voltage profiles in many of these designs were not satisfactory. Also, the PID design requires tuning of the gains for varying systems conditions.

This chapter presents the design of robust STATCOM controller. The design procedure starts by selecting a nominal operating point. The controller is designed so as to give satisfactory response over a set of perturbed plant. In the following a brief theory of the uncertainty model, the robust stability criteria, a graphical design technique termed as loop-shaping, which is employed to design the robust controller
are presented. These are followed by an algorithm. The material on this robust design is available in the literature [40, 41] and is presented here for completeness.

4.2 Uncertainty Modeling

Suppose that the nominal plant transfer function of a plant $P$ belongs to a bounded set of transfer function $\mathbf{P}$ and consider the perturbed transfer function because of the variations of its parameters can be expressed in the form,

$$\hat{P} = [1 + \Delta W_2]P$$

(4.1)

where

$\hat{P}$= A perturbed Plant transfer function

$\Delta$= A variable stable transfer function satisfying $||\Delta||_\infty \leq 1$

$W_2$= A fixed, stable and proper transfer function ( also called the weight )

Note: The infinity norm (or $\infty$-norm) of a function is the least upper bound of its absolute value.

It is assumed that no unstable or imaginary axis poles of $P(s)$ are canceled in the formation of $\hat{P}(s)$. Thus $P(s)$ and $\hat{P}(s)$ have the same unstable poles.

Since $\Delta$ accounts for phase uncertainty and its magnitude varies between 0 and 1 at all frequencies (i.e. acts as a scaling factor on the magnitude of the perturbation), $\mathbf{P}$ is the set of the transfer functions whose magnitude bode plot lies in the envelope surrounding the magnitude plot of $P(s)$, as illustrated in Fig. 4.1. Thus, the size of the unstructured uncertainty is represented by the size of the envelope containing $P$
Figure 4.1: Bode plot interpretation of multiplicative uncertainty.

Figure 4.2: Multiplicative uncertainty in the complex plane.
and is found to increase with increasing frequency. The upper edge of the envelope confirms to the plot of $(1 + |W_2(j\omega)||P(j\omega)|$ while the lower edge of the envelope confirms to the plot of $(1 - |W_2(j\omega)||P(j\omega)|$.

In the multiplicative uncertainty model [40], $\Delta W_2$ is the normalized plant perturbation away from 1. Hence, if $\| \Delta \|_\infty \leq 1$, then

$$\left| \frac{\hat{P}(j\omega)}{P(j\omega)} - 1 \right| \leq |W_2(j\omega)|$$

(4.2)

for all frequencies, so $|W_2(j\omega)|$ provides the uncertainty profile. As shown in Fig. 4.2 this inequality describes a closed disk in the complex plane of radius $|W_2(j\omega)|$ and centered at 1, which contains the point $\frac{\hat{P}(j\omega)}{P(j\omega)}$ for each frequency. The unstructured uncertainty is then represented by the closed disk and therefore the direction and phase of the uncertainty is left arbitrary.

### 4.3 Robust Stability

Consider a multi-input control system given in Fig. 4.3. Suppose that $P$ belongs to a set $\mathcal{P}$. The notion of robustness requires a controller, a set of plants and some characteristic of the system [40]. A controller $C$ provides robust stability if it provides internal stability for every plant in the uncertainty set $\mathcal{P}$. Hence, a test for robust stability involves the controller and the uncertainty set. Let $L$ denotes the open-loop transfer function (i.e. $L = PC$) and $S$ denotes the sensitivity function or the error to reference transfer function given by the following relation,

$$S = \frac{1}{1 + L}$$

(4.3)
Then the complimentary sensitivity function or the output to reference transfer function is given by

\[ T = 1 - S = \frac{L}{1+L} = \frac{PC}{1+PC} \]  

(4.4)

Furthermore, for a multiplicative perturbation model, the robust stability condition is met if and only if \( \| W_2T \|_\infty \leq 1 \) [40, 41]. A graphical interpretation of this condition is shown in Fig 4.4. Hence, the stability condition may be generalized as:

\[ \| W_2T \|_\infty \leq 1 \iff \left| \frac{W_2(j\omega)L(j\omega)}{1+L(j\omega)} \right| < 1, \text{ for all } \omega \]

\[ \iff |W_2(j\omega)L(j\omega)| < |1 + L(j\omega)|, \text{ for all } \omega \]

(4.5)

\[ \iff |\Delta(j\omega)W_2(j\omega)L(j\omega)| < |1 + L(j\omega)|, \text{ for all } \omega, \| \Delta \|_\infty \leq 1 \]  

(4.6)

Therefore the critical point, \(-1\), lies outside the disk, which is centered at \(L(j\omega)\) and radius \(|W_2(j\omega)L(j\omega)|\).

![Diagram](image)

**Figure 4.3:** Unity feedback plant with controller.

The relevance of the condition \( \| W_2T \|_\infty \leq 1 \) can be seen in its relation to the small-gain theorem, which states that the feedback system is initially stable if all the transfer functions (i.e. The plant \( P \), controller \( C \) and feedback gain \( F \)) are stable.
Figure 4.4: Robust stability condition in the complex plane

and \( \| PCF \|_\infty \leq 1 \). A block diagram of a typical perturbed system, ignoring all inputs, is shown in Fig 4.5. The transfer function from the output of \( \Delta \) to the input of \( \Delta \) equals \( -W_2 T \). The properties of the block diagram can be reduced to those of the configuration given in Fig 4.6. The maximum loop gain is \( \| -\Delta W_2 T \|_\infty \), which is less than 1 for all allowable \( \Delta \) if and only if the small-gain condition \( \| W_2 T \|_\infty \leq 1 \) holds.
4.4 Robust Performance

Internal stability and performance should hold for all plants in the uncertainty set $\mathbf{P}$ according to the generalization of robust performance. The robust stability condition for an internally stable, nominal feedback system is $\| W_2 T \|_\infty \leq 1$, and the nominal performance condition is $\| W_1 S \|_\infty \leq 1$, where $W_1$ is a real-rational, stable, minimum-phase transfer function (also called the weighting function) such that

$$\| W_1 S \|_\infty \leq 1 \iff \left| \frac{W_1(j\omega)}{1 + L(j\omega)} \right| < 1, \text{ for all } \omega$$

$$\iff |W_1(j\omega)| < |1 + L(j\omega)|, \text{ for all } \omega$$

(4.7)

If $\hat{P} = [1 + \Delta W_2]P$, then the perturbed sensitivity function is written as

$$\hat{S} = \frac{1}{1 + \hat{P}C} = \frac{1}{1 + (1 + \Delta W_2)PC} = \frac{1}{1 + (1 + \Delta W_2)L} = \frac{S}{1 + \Delta W_2 T}$$

(4.8)
Therefore, the robust performance condition is given by:

\[ \| W_2 T \|_\infty \leq 1 \text{ and } \left\| \frac{W_1 S}{1 + \Delta W_2 T} \right\|_\infty \leq 1 , \text{for all allowable } \Delta \] (4.9)

Since \(|\Delta| \leq 1\), then \(|-\Delta W_2 T| \leq |W_2 T|\). Thus \(|1 + \Delta W_2 T| \geq 1 - |W_2 T|\) for a fixed frequency, and it is then implied that

\[ \| \frac{W_1 S}{1 + \Delta W_2 T} \|_\infty \leq \left\| \frac{W_1 S}{1 - |W_2 T|} \right\|_\infty \leq 1 \] (4.10)

Hence Eq. (4.9) can be rewritten as a necessary and sufficient condition for robust performance, which is

\[ \| |W_1 S| + |W_2 T| \|_\infty \leq 1 \] (4.11)

Which is a stronger constraint than nominal performance or the robust stability condition alone. A graphical interpretation of this condition is shown in Fig. 4.7,
whereby

$$\| |W_1S| + |W_2T| \|_\infty \leq 1 \iff \left| \frac{W_1}{1 + L} \right| + \left| \frac{W_2L}{1 + L} \right| \leq 1, \text{ for all } \omega$$

$$\iff |W_1| + |W_2L| \leq 1 + L, \text{ for all } \omega \quad (4.12)$$

At each frequency, there exist two closed disks, one disk centered at -1, radius $W_1(j\omega)$

and the other centered at $L(j\omega)$, radius $|W_2(j\omega)L(j\omega)|$. The condition given by

Eq. (4.11) then holds if and only if the two disks have no nontrivial intersection (i.e. they can touch, but They cannot overlap).

It should be noted that since the condition for simultaneously achieving nominal performance and robust stability is

$$\| \max(|W_1S|, |W_2T|) \|_\infty \leq 1 \quad (4.13)$$

and the robust performance condition is tested by Eqn. (4.11), then the conditions in Eqn. (4.11) and (4.13) differ at most by a factor of two, In other words,

$$\| \max(|W_1S|, |W_2T|) \|_\infty \leq \| |W_1S| + |W_2T| \|_\infty \leq 2 \| \max(|W_1S|, |W_2T|) \|_\infty \quad (4.14)$$

The choice of these norms is not crucial, even though they may vary by as much as a factor of two. The inherent trade-off in control problems between $|W_1S|$ and $|W_2T|$ allow for similar solutions to be achieved even when using different norms.

### 4.5 Loop-shaping Technique

Loop-shaping is a graphical design procedure for robust performance design, whereby $P, W_1$ and $W_2$ are the input data, and a proper controller $C$ is designed to stabilize
Figure 4.7: Robust performance condition in the complex plane

the plant and satisfy Eq. (4.11) [40]. The basic idea of this method is to construct the loop transfer function $L$ to approximately satisfy Eqn.(4.11), and Then to attain $C$ via $C = \frac{L}{P}$. Internal stability of the nominal feedback system and the properness of $C$ constitute the constraints of this method. It is assumed that $P$ and $P^{-1}$ are both stable, otherwise $L$ must contain $P$'s unstable zeros and poles. Thus, the condition $L = PC$ must have no pole-zero cancellation. In terms of $W_1, W_2$, and $L$, Eq. (4.11) is given by

$$
\Gamma(j\omega) = | \frac{W_1(j\omega)}{1 + L(j\omega)} | + | \frac{W_2(j\omega)L(j\omega)}{1 + L(j\omega)} | < 1 \quad (4.15)
$$

which must hold for all frequencies. (Note that the argument $(j\omega)$ is dropped from this point onwards. The transfer functions are still functions of $(j\omega)$ unless otherwise
A necessary condition for robust performance is that at every frequency either $|W_1|$ or $|W_2|$ must be less than 1 [42]. Typically, $|W_1|$ is monotonically decreasing (for good tracking of low frequency signals) and $|W_2|$, is monotonically increasing (as uncertainty increases with increasing frequency). Hence, at each frequency, either $|W_1| < 1$ or $|W_2| < 1$. It is also the case when $|W_1| < 1$, $|W_2| \gg 1$. and when $|W_2| < 1$, $|W_1| \gg 1$. These properties can be used to determine the relationship between $|W_1|$, $|W_2|$, and $|L|$.

For the case $|W_1| \gg 1 > |W_2|$, Eq. (4.15) becomes

$$\Gamma < 1 \iff |W_1| + |W_2||L| < |1 + L|$$  \hspace{1cm} (4.16)

$$\Rightarrow |W_1| + |W_2||L| < 1 + |L|$$  \hspace{1cm} (4.17)

$$\Rightarrow |L| > \frac{|W_1| - 1}{1 - |W_2|}$$  \hspace{1cm} (4.18)

(a necessary condition), and because $|W_1| \gg 1$, it can be said that

$$|L| > \frac{|W_1| + 1}{1 - |W_2|} \iff |W_1| + |W_2||L| < |L| - 1$$  \hspace{1cm} (4.19)

$$\Rightarrow |W_1| + |W_2||L| < |L + 1|$$  \hspace{1cm} (4.20)

$$\Rightarrow \Gamma < 1$$

(a sufficient condition). Since $|W_1| \gg 1$, the condition $\Gamma < 1$ can be approximated by

$$|L| > \frac{|W_1|}{1 - |W_1|}$$  \hspace{1cm} (4.21)
For the case \(|W_1| < 1 \ll |W_2|\), Eq. (4.15)

\[
\Gamma < 1 \iff |W_1| + |W_2||L| < |1 + L| \tag{4.22}
\]

\[
\iff |W_1| + |W_2||L| < 1 + |L| \tag{4.23}
\]

\[
\implies |L| < \frac{1 - |W_1|}{|W_2| - 1} \tag{4.24}
\]

(a necessary condition). Since \(|W_2| \gg 1\), it can be said that

\[
|L| > \frac{1 - |W_1|}{|W_2| + 1} \iff |W_1| + |W_2||L| < 1 - |L| \tag{4.25}
\]

\[
\implies |W_1| + |W_2||L| < |1 + L| \tag{4.26}
\]

\[
\implies \Gamma < 1
\]

(a sufficient condition). Since \(|W_1| \gg 1\), the condition \(\Gamma > 1\) can be approximated by

\[
|L| < \frac{1 - |W_1|}{|W_2|} \tag{4.27}
\]

Therefore, because \(|W_1|\) is a decreasing function of frequency, and \(|W_2|\) is an increasing function, then typically at low frequencies,

\[
|W_1| > 1 > |W_2|
\]

and at high frequencies

\[
|W_1| < 1 < |W_2|
\]
At very high frequencies, let $|L|$ roll off at least as quickly as $|P|$ does. This ensures that the controller is proper. The general features of the open-loop transfer function are that the gain in the low frequency region should be large enough, and in the high frequency region, the gain should be attenuated as much as possible. The gain at the intermediate frequencies typically controls the gain and phase margins. Near the gain crossover frequency $\omega_c$, (where the magnitude equals 1), the slope of the log-magnitude curve in the Bode plot should be close to -20 dB/decade (i.e. the transition from low to high frequency should be smooth). If $|L|$ drops off too quickly through crossover, internal instability will result, so a gentle slope is crucial.

### 4.6 The Algorithm

The general algorithm for the loop-shaping design procedure can be outlined as [40]

- Obtain the db-magnitude plot for the nominal as well as perturbed plant transfer functions.

- Construct $W_2$ satisfying the constraint given in Eq. (4.2)

- On this plot, fit a graph of the magnitude of the open-loop transfer function $L$, whereby

$$|L| > \frac{|W_1|}{1 - |W_2|}$$

at low frequencies

and

$$|L| < \frac{1 - |W_1|}{|W_2|}$$

at high frequencies.
• Obtain a stable minimum-phase open-loop transfer function \( L \) for the gain \(|L|\) already constructed, normalizing so that \( L(O) > 0 \). The latter condition guarantees negative feedback.

• Recover the controller \( C \) from the condition \( L = PC \).

• Verify nominal stability and the condition of Eq. (4.11), i.e.
  \[ \| |W_1 S| + |W_2 T| \|_\infty \leq 1 \]

• Test for the internal stability by direct simulation of the closed loop transfer function for pre-selected disturbances or inputs.

• Repeat the procedure until satisfactory \( L \) and \( C \) are obtained. Note that a robust controller may not exist for all nominal conditions, and if it does, it may not be unique.
Chapter 5

Application of Loop-shaping Technique for Design of Robust STATCOM Controller

The principles and technique of using multiplicative uncertainties for modeling a plant, the robust stability and performance criteria, loop-shaping technique, etc. which were presented in the previous chapter has been employed to design robust controllers for STATCOM.
5.1 Robust Controller design for the approximate model

For designing the robust controller for the approximate model, the two controller functions $C_w$ and $C_v$ in the speed and voltage loops respectively were considered individually and then both of them together [43], as done in the case of PID controllers.

5.1.1 Robust Speed controller Design

The block diagram of the system in the absence of any control in the voltage feedback, and the absence of any input is shown in Fig. 5.1. Control in the speed loop alone is considered. The nominal operating point for the design was computed

\[ P = \frac{1.0435s}{(s + 50)(s^2 + 0.66s + 60.72)} \]  
(5.1)

Figure 5.1: Collapsed block diagram for robust speed feedback system.

for delivered power of 0.9 per unit at unity power factor. Off-nominal power outputs between 0.2-1.4 p.u. and power factors ratings between 0.8 lag - 0.8 lead were considered for the perturbed plant transfer functions. The nominal plant transfer function for the selected operating point is computed as
The db-magnitude vs. frequency response for the nominal and the perturbed plants is plotted in Fig. 5.2.

Figure 5.2: Nominal and perturbed plant transfer functions for robust speed feedback system.

From the relation $\left| \frac{P(j\omega)}{\hat{P}(j\omega)} - 1 \right| \leq W_2$, the quantity $\left| \frac{P(j\omega)}{\hat{P}(j\omega)} - 1 \right|$ for each perturbed plant is constructed and the uncertainty profile is fitted to the function

$$W_2(s) = \frac{0.8s^2 + 2.24s + 39.2}{(s^2 + 0.98s + 49)}$$  \hspace{1cm} (5.2)

This is shown in Fig. 5.2

A butterworth filter satisfies all the properties of for $W_1(s)$ and is written as

$$W_1(s) = \frac{K_d f_c^2}{(s^3 + 2s^2 f_c + 2sf_c^2 + f_c^3)}$$  \hspace{1cm} (5.3)
Figure 5.3: The uncertainty profile for the approximate model.

\( K_d \) and \( f_c \) are selected as 0.01 and 1 respectively.

For given \( W_1 \) and \( W_2 \), the open loop transfer function \( L \) is selected by trial and error to fit the relations that at low frequency \( |L(s)| > \frac{|W_2|}{1-|W_2|} \), and for high frequency \( |L(s)| < \frac{1}{|W_2|} \). It should also satisfy the robust stability criteria \( \|W_1 S + W_2 T\|_\infty < 1 \) and nominal performance criterion \( \|W_1 S\|_\infty < 1 \). The open loop transfer function \( L \) that satisfies loop-shaping criteria has been obtained as

\[
L(s) = \frac{208.75(s + 1)(s + 2)}{(s + 0.01)(s + 50)(s^2 + 0.66s + 60.72)}
\] (5.4)

The db magnitude for \( L \) satisfying the conditions is shown Fig. 5.4. The plots for the nominal performance and robust performance criteria are shown in Fig. 5.5. As shown in the Figure, that the curve for \( \|W_1 S + W_2 T\| \) is always less than 0 db
Figure 5.4: Loop shaping plots relating $W_1$, $W_2$ and $L$ for robust speed controller.

Figure 5.5: Robust and nominal performance criteria for robust speed controller.
and thus satisfying the relation robust stability and the performance criterion. The nominal performance criteria \(|W_1S|\leq 1\) is also satisfied.

For the above open loop transfer function, the controller function was found from the relation

\[
C(s) = \frac{L(s)}{P(s)}
\]

and is given as

\[
C_w(s) = \frac{200(s + 1)(s + 2)}{s(s + 0.01)}
\]

The robust STATCOM speed controller was tested by applying an input torque pulse of 100\% of 5 ms. duration to the generator shaft. For a number of operating conditions, simulation results for the STATCOM bus voltage and variation in the rotor angle are given in Fig. 5.6 - 5.7 respectively. Curve a represents the nominal operating condition.

Fig. 5.6 shows the STATCOM bus voltage variations for a) \(P_o = P_o = 0.9\) p.u. at unity power factor, b) \(P_o = 1.0\) p.u. at 0.95 lagging power factor, c) \(P_o = 1.1\) p.u. at 0.95 leading power factor, d) \(1.2\) p.u. at 0.98 leading power factor, and e) \(P_o = 0.5\) p.u. at 0.95 lagging power factor. The corresponding rotor angle variations are given in Fig. 5.7. From the figures, it can be observed that a very good damping properties can be obtained with the robust speed controller over a wide range of operating conditions.

Figures 5.8 and 5.9 shows the variations in the generator angular speed and the controller current output for even more largely varied operating conditions. Results
Figure 5.6: STATCOM bus voltage with robust speed controller.

Figure 5.7: Rotor angle corresponding to Fig 5.6.
Figure 5.8: % Angular speed deviation with robust speed controller.

Figure 5.9: Controller output current corresponding to Fig.5.8
confirms that the designed STATCOM speed controller is robust to handle large variations in the system.

5.1.2 Robust controller in the voltage loop alone

The block diagram corresponding to Fig. 5.1. with the voltage loop controller is shown in Fig. 5.10. The nominal plant transfer function for this formulation is

\[ P = \frac{-10.35(s^2 + 0.667s + 68.0233)}{(s + 50)(s^2 + 0.667s + 61.7585)} \] (5.7)

Because of the sign of the \( P \), the nominal plant is in a positive feedback loop. Such a system does not fall in the category of the internal stability [40] and robustness criterion cannot be applied as such. However, by forcing \( C_v \) to take the opposite polarity, a robust controller was designed following the procedure outlined in section 5.1.1. The controller does provide reasonable amount of damping over a range of operating conditions, but it is not as effective as the speed controller \( C_w \). It is noted that earlier studies also revealed that the STATCOM voltage control loop does not provide enough damping [16, 37] and similar observation was found by the application of the PID controller in the voltage loop alone in section 3.2.2. PI
controller design is often unsatisfactory, and may even lead to unstable situation [37]. This can be attributed to the fact that there is a pair of poles and a pair of zeros is $P$ on the imaginary axis, which are in close proximity. These pole-zero pairs are responsible for the oscillatory nature of the response in that voltage loop which is a desirable for voltage regulation purpose.

### 5.1.3 Voltage-speed Robust controller

In the following section, a robust design for a controller in the speed loops is presented which retains a nominal voltage feedback gain $C_v = 1$.

The nominal plant transfer function with robust controller in the speed loop and including the voltage feedback can be expressed as

$$P = \frac{1.1975s^2}{(s + 58.3475)(s^2 + 2.672s + 10.9579)} \tag{5.8}$$

Note that positive feedback situation disappears allowing a proper robust design.

Continuing the same design procedure employed in section 5.1.1, considering the same transfer functions for $W_1$, $W_2$ as given in Eq. (5.3) and (5.2), a choice of the open loop transfer function,

$$L(s) = \frac{175(s + 6)(s + 0.8)}{(s + 58.3475)(s^2 + 5s + 49)} \tag{5.9}$$

with the resulting control function,

$$C_w(s) = \frac{146.13(s + 6)(s + 0.8)(s^2 + 2.672s + 10.9579)}{s^2(s^2 + 5s + 49)} \tag{5.10}$$

provides excellent damping control over a wide range of operating conditions. Fig. 5.11. shows the db-magnitude plot relating $W_1$, $W_2$ and $L$, which was employed
to arrive at the controller of Eq. 5.10. The plots for the nominal and robust performance criteria are shown in Fig. 5.12.

The system model has been simulated for 100% mechanical torque pulse of 5 ms duration. Five different loading conditions have been considered to investigate the robustness of the designed controller. The variations in generator rotor angle and the bus voltage are shown in Figures 5.13 and 5.14 respectively. As can be observed, the robust controller provides excellent damping characteristics and keeping the bus voltage to an acceptable value. However for the operating condition away from the nominal operating point, an oscillatory response has been observed which damps with the time shown by curve e in Fig. 5.14 for 0.5 p.u power output at 0.95 lagging power factor.

5.2 Robust Controller design for detailed model

There are two possible controls in the detailed model of STATCOM as shown in Fig 2.9. These are the magnitude of the STATCOM voltage (c) and its phase (ψ). In chapter 3, it was shown that the controller in the phase angle control loop does not provide any extra damping. This is somewhat similar to the controller $C_\psi$ in the approximate model.

Since the phase control does not provide extra damping, $C_\psi$ was set to a nominal value of 1 for designing the robust magnitude controller. The nominal plant transfer function $P$ is taken for power output of 0.9 at unity power factor load and is obtained
Figure 5.11: Loop shaping plots relating $W_1$, $W_2$ and $L$ for voltage-speed robust controller.

Figure 5.12: Robust and nominal performance criteria for voltage-speed robust controller.
Figure 5.13: Rotor angle with robust controller for voltage-speed robust controller

Figure 5.14: STATCOM bus voltage corresponding to Fig. 5.13
as,

\[
P = \frac{0.2466s^2(s + 100.774)(s - 0.214309)}{(s + 99.1923)(s + 1.0901)(s + 0.0527)(s^2 + 0.65484s + 21.4956)}
\]  

(5.11)

The collapsed block diagram for only magnitude control is shown in Fig. 5.15. The db magnitude vs. frequency plot for the nominal and perturbed plants are shown in Fig. 5.16. From this plot the quantity \[ \frac{P(j\omega)}{P(j\omega)} - 1 \] is constructed and is shown in Fig. 5.17. Off nominal operating points for output power ranges from 0.8 p.u to 1.4 p.u and power factor from 0.8 lagging to 0.8 leading were considered. The function \( W_2 \) fitting the relationship \[ |\frac{P(j\omega)}{P(j\omega)} - 1| \leq |W_2(j\omega)| \] is constructed as

\[
W_2(s) = \frac{2.165s^2 + 4.221s + 27.44}{(2.5s^2 + 2.436s + 18.92)}
\]  

(5.12)

![Collapsed block diagram for robust \( c \) controller.](image)

The function \( W_1 \) was selected as,

\[
W_1(s) = \frac{K_df_c^2}{(s^3 + 2s^2f_c + 2sf_c^2 + f_c^3)}
\]  

(5.13)

\( K_d \) and \( f_c \) were selected to 0.01 and 1 respectively. The open loop transfer function \( L \) which satisfies the loop-shaping criteria was found to be

\[
L(s) = \frac{0.5(s + 0.009)(s + 100.774)(s - 0.214309)(s + 1)}{(s + 12)(s + 0.0901)(s + 0.01)(s^2 + 0.65485s + 21.4956)}
\]  

(5.14)
Figure 5.16: nominal and perturbed plant transfer functions for robust speed feedback system.

The db vs. frequency plots relating relating $L$, $W_1$ and $W_2$ is show in Fig. 5.18. Fig. 5.19 shows the plots for the nominal and robust performance criterion. From the relation $L = PC$, the controller transfer function was constructed as

$$C_c(s) = \frac{2.0273(s + 1)(s + 1.0901)(s + 0.0527)(s + 99.19233)(s + 0.009)}{s^2(s + 12)(s + 0.0901)(s + 0.01)} \quad (5.15)$$

The controller was tested by simulating the detailed model for a disturbance of 100% input torque pulse of 10 ms duration. The simulations results obtained for a number of operating conditions are given in Fig. 5.20 - 5.21. The responses recorded are the variations in the rotor angle and mid-bus respectively. Fig. 5.20 shows the rotor angle variation for the following operating conditions. a) Nominal operating
Figure 5.17: the uncertainty profile for detailed model.

condition, b) Unity power output at 0.95 lagging power factor. Curve c and d shows the responses at power output of 0.5 and 1.2 respectively with the corresponding power factors of 0.95 lagging and 0.98 leading. It was observed that the designed magnitude control provides damping for all the operating conditions. Expectedly, the response of the states farther away from the nominal are not as good. This is exhibited by a slightly oscillatory response for 0.5 p.u output shown by curve c.

Fig. 5.21 shows the corresponding variations in the mid bus voltage. The robust controller maintains the STATCOM bus voltage to its desired value faithfully. The maximum transient overshoot observed was about 10%
Figure 5.18: Loop shaping plots relating $W_1$, $W_2$ and $L$ for detailed model Robust controller.

Figure 5.19: Robust and nominal performance criteria for detailed model Robust controller.
Figure 5.20: Rotor angle with robust controller for detailed model.

Figure 5.21: STATCOM bus voltage corresponding to Fig. 5.20.
5.2.1 Fault studies for the detailed model with Robust controller

The robust controller designed was tested for a three phase fault for 0.1 sec at the infinite bus of the power system. Figures 5.22 - 5.23 shows the generator rotor angle and STATCOM bus voltage variations for a wide range of power output conditions. The following cases has been considered. a) Nominal operating conditions, b) 1.0 p.u at 0.95 lagging power factor, c) 0.5 p.u. at 0.95 lagging power factor and d) 1.2 power output at 0.98 leading power factor.

The response shows that even for very heavily overloaded condition of $P_o = 1.2$ p.u. STATCOM bus voltage transient overshoot is less than 10 %. The electromechanical and electrical transients are controlled virtually in one or two oscillations with the robust controller. Even for large disturbances of 0.15 sec duration fault, the robust controller is able to stabilize the system. The voltage variations, however, are large.

The controller is designed to give robust performance for operating conditions near the nominal one. For operating conditions off the nominal one, the response may not be as good as depicted by curve c in Fig 5.22.
Figure 5.22: Rotor angle variation with robust controller for the detailed model (for three phase fault at infinite bus.)

model (for 3 phase fault at infinite bus.)

Figure 5.23: STATCOM bus voltage variation corresponding to Fig. 5.22.)
Chapter 6

Conclusions and Future Work

The dynamic behaviour of a single machine infinite bus power system installed with a STATCOM at the mid-point of the transmission line has been investigated in this thesis. Dynamic models has been derived for the approximate and the detailed representations of the power system. Comparative study for the different combinations of PID controller has been presented for both the models.

For the approximate model, two control inputs has been identified, one in the speed loop and the other in the voltage loop. It has been found that controller in the voltage loop alone is not effective in providing damping to the system but its presence is found to be necessary for the voltage regulation. A controller in the speed loop has effective control over the electrical and electro-mechanical transients. For a nominal unity gain in the voltage loop, a PD controller in the speed loop gave reasonably good damping characteristics.

For the detailed model also two control inputs to the STATCOM has been iden-
tified, one is the magnitude and the other is the phase for the STATCOM control voltage. It was observed that PID control for phase alone is not effective in providing damping. The proportional controller was observed to provide damping to the system but other transient indices were poor. The PID control was generally not found satisfactory in terms of both steady state and transient performance.

A novel method of designing robust damping control strategies for STATCOM controller is proposed for both the approximate and detailed models. The controller designed was tested for a number of disturbance conditions including symmetrical three-phase faults. The robust design has been found to be very effective for a range of operating conditions of the power system. The operating conditions for which the controller provides good performance depends on the spectrum of perturbed plants selected in the design process. The robust design has been found to be superior to the conventional PI controllers, where the controller coefficient normally need to be retuned for various operating conditions. The graphical loop-shaping method is simple and straightforward to implement.

The robust STATCOM controller designed through both the approximate and exact models did provide extra damping to the system. The design through the approximate model is simple in terms of the dimension, and was carried out as an initial study. Detailed study was more sensitive to variations of AVR and controller DC voltages.
6.1 Recommendations for future work

In the following, some recommendations are given for future research in the area.

- Further research is needed to evaluate the impact of phase angle ($\psi$) control of STATCOM voltage for the dynamic performance of the system.

- The effect of STATCOM on a multimachine system stability needs investigation. The location(s) of the STATCOM device(s) in a multimachine system requires careful study.

- In this study SMIB system with STATCOM located at the mid-point of the transmission line was considered. The impact of the location of the STATCOM other than mid-point of the transmission line on the dynamic performance can also be studied.

- The robust controller design of STATCOM for damping control with other FACTS devices such as unified power flow controller (UFPC) and static synchronous series compensator SSSC, etc. also needs investigation.
Appendix A

Derivation of the Simplified Dynamic Model of SMIB installed with STATCOM

Figure A.1: Equivalent Circuit Diagram of the System of fig. 2.5
From Fig. A.1

\[ i_2 = i_1 + I_S \quad (A.1) \]

Now

\[ V_m = V_i - j i_1 X_1 \quad (A.2) \]
\[ V_m = V_b + j i_2 X_2 \quad (A.3) \]

Equating equation A.2 and A.3 and substituting the value of \( i_2 \):

\[ V_i - j i_1 X_1 = V_b + j X_2 (i_1 + i_S) \quad (A.4) \]

But

\[ V_i = V_d + j V_q \quad (A.5) \]
\[ V_i = x_q i_1 q + j (e_q' - x_d' i_1 d) \quad (A.6) \]
\[ i_1 = i_1 d + j i_1 q \quad (A.7) \]
\[ i_S = I_S \cos \theta - j I_S \sin \theta \quad (A.8) \]

where \( \theta \) is the angle of the mid bus or STATCOM bus.

\[ V_b = V \sin \delta + j V \cos \delta = V_{bd} + j V_{bq} \quad (A.9) \]

where \( \delta = \) load angle.

Substituting all into equation A.4

\[ x_q i_1 q + j (e_q' - x_d' i_1 d) - j (i_1 d + j i_1 q) X_1 = \]
\[ V_{bd} + j V_{bq} + j X_2 [i_1 d + j i_1 q + I_S \cos \theta - j I_S \sin \theta] \quad (A.10) \]
\[(X_1 + x_q)i_{1q} + j[e'_q - x'_{d1}i_{1d} - X_1i_{1d}] =

V_{bd} - X_2i_{1q} + I_S\sin\theta + j[V_{bq} + X_2i_{1d} + X_2I_S\cos\theta]
\] (A.11)

Comparing the real and imaginary parts.

From Real part:

\[(x_q + X_1)i_{1q} = V_{bd} - X_2i_{1q} + I_S\sin\theta\] (A.12)

\[i_{1q} = \frac{V_{bd} + I_S\sin\theta}{X_1 + X_2 + x_q}\] (A.13)

and from Imaginary part:

\[e'_q - (x'_d + X_1)i_{1d} = V_{bq} + X_2i_{1d} + X_2I_S\cos\theta\] (A.14)

\[i_{1d} = \frac{e'_q - V_{bq} - X_2I_S\cos\theta}{X_1 + X_2 + x'_d}\] (A.15)

Expression for \(V_m\):

from equation A.3

\[V_m = V_b + ji_2X_2\] (A.16)

\[V_{md} + jV_{mq} = V_{bd} + jV_{bq} + j(i_{1d} + ji_{1q} + I_S\cos\theta - jI_S\sin\theta)X_2\] (A.17)

\[V_{md} + jV_{mq} = (V_{bd} - X_2i_{1q} + X_2I_S\sin\theta) + j(V_{bq} + X_2i_{1d} + X_2I_S\cos\theta)\] (A.18)

Comparing real and imaginary parts:

\[V_{md} = V_{bd} - (i_{1q} - I_S\sin\theta)X_2\] (A.19)

\[V_{mq} = V_{bq} + (i_{1d} + I_S\cos\theta)X_2\] (A.20)
Substituting the value of $i_{1d}$ and $i_{1q}$ from equation A.13 and A.15:

\[
V_{md} = V_{bd} - \left[ \frac{V_{bd} + I_S X_2 \sin \theta}{X_1 + X_2 + x_q} - I_S \sin \theta \right] X_2 \tag{A.21}
\]

\[
V_{md} = V_{bd} - \left[ \frac{V_{bd} + I_S X_2 \sin \theta - (X_1 + X_2 + x_q) I_S \sin \theta}{X_1 + X_2 + x_q} \right] X_2 \tag{A.22}
\]

\[
V_{md} = V_{bd} - \left[ \frac{V_{bd} - (X_1 + x_q) I_S \sin \theta}{X_1 + X_2 + x_q} \right] X_2 \tag{A.23}
\]

\[
V_{md} = \frac{(V_{bd} + X_2 I_S \sin \theta)(X_1 + x_q)}{X_1 + X_2 + x_q} \tag{A.24}
\]

Similarly,

\[
V_{mq} = V_{bq} + \left[ \frac{e_q' - V_{bq} - X_2 I_S \cos \theta}{X_1 + X_2 + x_d'} + I_S \cos \theta \right] X_2 \tag{A.25}
\]

\[
V_{mq} = \frac{e_q' + V_{bq}(X_1 + x_d') + (X_1 + x_d')X_2 I_S \cos \theta}{X_1 + X_2 + x_d'} \tag{A.26}
\]

The non-linear model is given by the following equations:

\[
\dot{\delta} = \omega_b \omega \tag{A.27}
\]

\[
\dot{\omega} = \frac{1}{M} [P_m - P_e - D \omega] \tag{A.28}
\]

\[
\dot{I}_S = \frac{1}{T} [-I_S + Ku] \tag{A.29}
\]

where

\[
P_e = \frac{e_q' V_m \sin \theta + \frac{V_m^2}{2} \frac{x_d' - x_q}{(x_d' + X_1)(x_q + X_1)} \sin 2\theta}{x_d' + X_1} \tag{A.30}
\]

\[
V_{md} = \frac{(X_1 + x_q) V \sin \delta + I_S X_2 \sin \theta (X_1 + x_q)}{X_1 + X_2 + x_q} \tag{A.31}
\]

\[
V_{mq} = \frac{(X_1 + x_d') V \cos \delta + e_q' X_2 + I_S X_2 \cos \theta (X_1 + x_d')}{X_1 + X_2 + x_d'} \tag{A.32}
\]

\[
V_m = V_{md} + j V_{mq} \tag{A.33}
\]

\[
\theta = \tan^{-1} \left( \frac{V_{md}}{V_{mq}} \right) \tag{A.34}
\]
For Linear Model:

\[
\tan \theta = \frac{V_{md}}{V_{mq}} \tag{A.35}
\]

\[
\tan \theta = \frac{X_1 + X_2 + x_d'}{X_1 + X_2 + x_q} \times \left( \frac{(X_1 + x_q)V \sin \delta + I_S X_2 \sin \theta (X_1 + x_q)}{(X_1 + x_d')V \cos \delta + e_q' X_2 + X_2 (X_1 + x_d')I_S \cos \theta} \right) \tag{A.37}
\]

Let

\[
d_1 = \frac{X_1 + X_2 + x_d'}{X_1 + X_2 + x_q} \tag{A.38}
\]

\[
d_2 = (X_1 + x_q)V \tag{A.39}
\]

\[
d_3 = X_2 (X_1 + x_q) \tag{A.40}
\]

\[
d_4 = e_q' X_2 \tag{A.41}
\]

\[
d_5 = (X_1 + x_d')V \tag{A.42}
\]

\[
d_6 = X_2 (X_1 + x_d') \tag{A.43}
\]

\[
\tan \theta = \frac{d_1 d_2 \sin \delta + d_3 I_S \sin \theta}{d_4 + d_5 \cos \delta + d_6 I_S \cos \theta} \tag{A.44}
\]

By Cross multiplication:

\[
d_4 \tan \theta + d_5 \tan \theta \cos \delta + d_6 I_S \sin \theta = d_1 d_2 \sin \delta + d_1 d_3 I_S \sin \theta \tag{A.46}
\]

\[
d_4 \tan \theta + d_5 \tan \theta \cos \delta + (d_6 I_S - d_1 d_3 I_S) \sin \theta = d_1 d_2 \sin \delta \tag{A.47}
\]

Differentiating equation A.47 with respect to \( \delta \) assuming \( \theta \) depends on \( \delta \)

\[
d_4 \sec^2 \theta \frac{\partial \theta}{\partial \delta} + d_5 \cos \delta \sec^2 \theta \frac{\partial \theta}{\partial \delta} + d_5 \tan \theta (- \sin \delta) +
\]

\[
(d_6 I_S - d_1 d_3 I_S) \cos \theta \frac{\partial \theta}{\partial \delta} = d_1 d_2 \cos \delta \tag{A.48}
\]
\[
\left[ d_4 \sec^2 \theta + d_5 \cos{\delta} \sec^2 \theta + (d_6 I_S - d_1 d_3 I_S) \cos{\theta} \right] \frac{\partial{\theta}}{\partial{\delta}} = d_1 d_2 \cos{\delta} + d_5 \tan{\theta} \sin{\delta} \tag{A.49}
\]

Let

\[
d_7 = d_4 \sec^2 \theta + d_5 \cos{\delta} \sec^2 \theta + (d_6 I_S - d_1 d_3 I_S) \cos{\theta} \tag{A.50}
\]

Therefore, equation A.50 becomes:

\[
\frac{\partial{\theta}}{\partial{\delta}} = \frac{1}{d_7} \left[ d_1 d_2 \cos{\delta} + d_5 \tan{\theta} \sin{\delta} \right] \tag{A.51}
\]

Similarly differentiating equation A.47 with respect to \( I_S \) assuming \( \theta \) depends on \( I_S \):

\[
d_4 \sec^2 \theta \frac{\partial{\theta}}{\partial{I_S}} + d_5 \cos{\delta} \sec^2 \theta \frac{\partial{\theta}}{\partial{I_S}} + (d_6 I_S - d_1 d_3 I_S) \cos{\theta} \frac{\partial{\theta}}{\partial{I_S}} + \\
\sin{\theta}(d_6 - d_4 d_3) = 0 \tag{A.52}
\]

\[
\left[ d_4 \sec^2 \theta + d_5 \cos{\delta} + (d_6 I_S - d_1 d_3 I_S) \cos{\theta} \right] \frac{\partial{\theta}}{\partial{I_S}} = \sin{\theta}(d_1 d_3 - d_6) \tag{A.53}
\]

\[
\frac{\partial{\theta}}{\partial{I_S}} = \frac{1}{d_8} (d_1 d_3 - d_6) \tag{A.54}
\]

where

\[
d_8 = d_4 \sec^2 \theta + d_5 \cos{\delta} + (d_6 I_S - d_1 d_3 I_S) \cos{\theta} \tag{A.55}
\]

By linearizing equation A.31, A.32 and A.33, around equilibrium point. We got

\[
\Delta V_m = K_{V_m \delta} \Delta \delta + K_{V_m I_S} \Delta I_S \tag{A.56}
\]
and

\[ \Delta P_e = K_{P_e \delta} \Delta \delta + K_{P_e I_S} \Delta I_S \]  \hspace{1cm} (A.57)

where

\[ K_{V_m \delta} = \frac{\partial V_m}{\partial \delta} \]  \hspace{1cm} (A.58)

\[ K_{V_m I_S} = \frac{\partial V_m}{\partial I_S} \]  \hspace{1cm} (A.59)

\[ K_{P_e \delta} = \frac{\partial P_e}{\partial \delta} \]  \hspace{1cm} (A.60)

\[ K_{P_e I_S} = \frac{\partial P_e}{\partial I_S} \]  \hspace{1cm} (A.61)

Calculating the coefficients

\[ K_{P_e \delta} = \frac{\partial P_e}{\partial \delta} \]  \hspace{1cm} (A.62)

\[ K_{P_e \delta} = \frac{\partial P_e \partial \delta}{\partial \theta \partial \delta} \]  \hspace{1cm} (A.63)

\[ K_{P_e \delta} = \frac{\partial}{\partial \delta} \left[ \frac{e_q' V_m}{X_1 + x_d} \sin \theta + \frac{V_m^2 (x_d' - x_q)}{2 (x_d' + X_1)(x_q + X_1)} \sin 2\theta \right] \times \]

\[ \frac{1}{d_7} [d_5 \tan \theta \sin \delta + d_1 d_2 \cos \delta] \]  \hspace{1cm} (A.64)

\[ K_{P_e \delta} = \frac{1}{d_7} \left[ \frac{e_q' V_m}{X_1 + x_d} \cos \theta + \frac{V_m^2 (x_d' - x_q)}{(x_d' + X_1)(x_q + X_1)} \cos 2\theta \right] \times \]

\[ [d_5 \tan \theta \sin \delta + d_1 d_2 \cos \delta] \]  \hspace{1cm} (A.65)

Similarly,

\[ K_{P_e I_S} = \frac{\partial P_e}{\partial I_S} \]  \hspace{1cm} (A.66)

\[ = \frac{\partial P_e \partial \theta}{\partial \theta \partial I_S} \]  \hspace{1cm} (A.67)
\[ K_{PdI_S} = \frac{1}{d_3} \left[ \frac{e_q V_m}{e_1 + e_q} \cos \theta + \frac{V_m^2 \left( e_1 - e_q \right)}{e_1 + e_q} \cos 2\delta \right] [d_4 d_5 - d_6] \sin \theta \] (A.68)

In order to obtain \( \frac{\partial V_m}{\partial \delta} \) and \( \frac{\partial V_m}{\partial I_S} \), applying the relation for the magnitude of the mid bus voltage \( V_m \):

\[ V_m^2 = V_{md}^2 + V_{mq}^2 \] (A.69)

Differentiating partially with respect to \( \delta \) and \( I_S \)

\[ V_m \frac{\partial V_m}{\partial \delta} = V_{md} \frac{\partial V_{md}}{\partial \delta} + V_{mq} \frac{\partial V_{mq}}{\partial \delta} \] (A.70)

\[ V_m \frac{\partial V_m}{\partial I_S} = V_{md} \frac{\partial V_{md}}{\partial I_S} + V_{mq} \frac{\partial V_{mq}}{\partial I_S} \] (A.71)

where

\[ \frac{\partial V_{md}}{\partial \delta} = \left( \frac{X_1 + X_q}{X_1 + X_2 + X_q} \right) V \cos \delta + \frac{I_S X_2 (X_1 + X_q)}{X_1 + X_2 + X_q} \cos \theta \frac{\partial \theta}{\partial \delta} \] (A.72)

\[ \frac{\partial V_{md}}{\partial \delta} = \left( \frac{X_1 + X_q}{X_1 + X_2 + X_q} \right) V \cos \delta + \frac{I_S X_2 (X_1 + X_q)}{X_1 + X_2 + X_q} \times \]
\[ \cos \theta \frac{1}{d_7} [d_5 \tan \theta \sin \delta + d_1 d_2 \cos \delta] \] (A.73)

and

\[ \frac{\partial V_{mq}}{\partial \delta} = \frac{1}{X_1 + X_2 + x_d} \left[ -(X_1 + x_d' V \sin \delta - I_S X_2 (X_1 + x_d') \sin \theta \times \right. \]
\[ \left. \frac{1}{d_7} \left( d_5 \tan \theta \sin \delta + d_1 d_2 \cos \delta \right) \right] \] (A.74)

\[ \frac{\partial V_{mq}}{\partial \delta} = - \frac{(X_1 + x_d')}{(X_1 + X_2 + x_d')} \left[ V \sin \delta + \frac{I_S X_2 \sin \theta}{d_7} \cdot (d_5 \tan \theta \sin \delta + d_1 d_2 \cos \delta) \right] \] (A.75)
\[
\begin{align*}
\frac{\partial V_{md}}{\partial I_S} &= \frac{1}{X_1 + X_2 + x_q} \left[ X_2 (X_1 + x_q) \sin \theta + I_S X_2 (X_1 + x_q) \cos \theta \cdot \frac{\partial \theta}{\partial I_S} \right] \\
&= \frac{(X_1 + x_q) X_2}{X_1 + X_2 + x_q} \left[ \sin \theta + \frac{I_S}{d_8} \cdot \cos \theta \cdot (d_1 d_3 - d_6) \sin \theta \right]
\end{align*}
\]  

(A.76)

(A.77)

Similarly

\[
\begin{align*}
\frac{\partial V_{mq}}{\partial I_S} &= \frac{1}{X_1 + X_2 + x_d'} \left[ X_2 (X_1 + x_d') \cos \theta - I_S X_2 (X_1 + x_d') \sin \theta \cdot \frac{\partial \theta}{\partial I_S} \right] \\
&= \frac{(X_1 + x_d') X_2}{X_1 + X_2 + x_d'} \left[ \cos \theta - \frac{I_S}{d_8} \cdot \sin \theta \cdot (d_1 d_3 - d_6) \sin \theta \right]
\end{align*}
\]  

(A.78)

(A.79)

Substituting back into equation A.70 and A.71

\[
K_{V_m}\delta = \frac{\partial V_m}{\partial \delta}
\]  

(A.80)

\[
K_{V_m}\delta = \frac{V_{md}}{V_m} \cdot \frac{(X_1 + x_q)}{(X_1 + X_2 + x_q)} \left[ V \cos \delta + \frac{1}{d_7} I_S X_2 \cos \theta (d_5 \tan \theta \sin \delta + d_1 d_2 \cos \delta) \right] \\
- \frac{V_{mq}}{V_m} \cdot \frac{(X_1 + x_d')}{(X_1 + X_2 + x_d')} \left[ V \sin \delta + \frac{1}{d_7} I_S X_2 \sin \theta (d_5 \tan \theta \sin \delta + d_1 d_2 \cos \delta) \right]
\]  

(A.81)

\[
K_{V_m}I_S = \frac{\partial V_m}{\partial I_S}
\]  

(A.82)

\[
K_{V_m}I_S = \frac{V_{md}}{V_m} \cdot \frac{(X_1 + x_q) X_2}{(X_1 + X_2 + x_q)} \left[ \sin \theta + \frac{1}{d_8} I_S \cos \theta (d_1 d_3 - d_6) \sin \theta \right] \\
+ \frac{V_{mq}}{V_m} \cdot \frac{(X_1 + x_d') X_2}{(X_1 + X_2 + x_d')} \left[ \cos \theta - \frac{1}{d_8} I_S \sin \theta (d_1 d_3 - d_6) \sin \theta \right]
\]  

(A.83)
Appendix B

Derivation of the Detailed
Dynamic Model of SMIB installed with STATCOM

The voltage and current relationship for the power system with STATCOM shown in Fig. B.1 are expressed as

\[ \dot{I}_{Lo} = \dot{I}_{Loxd} + j \dot{I}_{Loq} \]

\[ V_o = cV_{DC}(\cos \psi + j \sin \psi) = cV_{DC} \angle \psi \]  \hspace{1cm} (B.1)

\[ \frac{dV_{DC}}{dt} = \frac{I_{DC}}{C_{DC}} = \frac{c}{C_{DC}} (I_{Loxd} \cos \psi + I_{Loq} \sin \psi) \]  \hspace{1cm} (B.2)
Figure B.1: STATCOM installed in a single machine infinite bus power system.

where

\[ c = mk \]

\[ k = \frac{\text{AC Voltage}}{\text{DC Voltage}} \]

\[ m = \text{modulation ratio defined by PWM} \]

\[ \psi = \text{defined by PWM} \]

From Fig. B.1,

\[ \vec{V}_t = jX_{IL}I_L + jX_{LB}I_{LB} + \vec{V}_B \]  \hspace{1cm} (B.3)
Now

\[ I_{LB} = I_{tL} - I_{Lo} \]  \hspace{1cm} (B.4)

\[ I_{Lo} = \frac{\bar{V}_{L} - \bar{V}_{o}}{jX_{SDT}} \]  \hspace{1cm} (B.5)

\[ \bar{V}_{L} = \bar{V}_{t} - X_{iL}I_{tL} \]  \hspace{1cm} (B.6)

Substituting in the expression for \( I_{LB} \)

\[ I_{LB} = I_{tL} - \frac{V_{t} - jX_{tL}I_{tL} - V_{o}}{jX_{SDT}} = \frac{jX_{SDT}I_{tL} - V_{t} + jX_{tL}I_{tL}}{jX_{SDT}} \]  \hspace{1cm} (B.7)

Eq. B.4 becomes

\[ V_{t} = jX_{tL}I_{tL} + \frac{jX_{LB}}{jX_{SDT}}(jI_{tL}X_{SDT} - \bar{V}_{t} + jX_{tL}I_{tL} + V_{o}) \]  \hspace{1cm} (B.8)

\[ V_{t} = jX_{tL}I_{tL} + jX_{LB}I_{tL} - \frac{X_{LB}}{X_{SDT}}\bar{V}_{t} + \frac{jX_{tL}X_{LB}}{X_{SDT}}I_{tL} + \frac{X_{LB}}{X_{SDT}}V_{B} \]  \hspace{1cm} (B.9)

\[ \left(1 + \frac{X_{LB}}{X_{SDT}}\right)\bar{V}_{t} - \frac{X_{LB}}{X_{SDT}}V_{o} - \bar{V}_{B} = j\left(X_{tL} + X_{LB} + \frac{X_{tL}}{X_{SDT}}\right)I_{tL} \]  \hspace{1cm} (B.10)

Let

\[ Z = \left(1 + \frac{X_{LB}}{X_{SDT}}\right) \]  \hspace{1cm} (B.11)

\[ A = \left(X_{tL} + X_{LB} + \frac{X_{tL}}{X_{SDT}}\right) \]  \hspace{1cm} (B.12)

\[ Z\bar{V}_{t} - \frac{X_{LB}}{X_{SDT}}V_{o} - \bar{V}_{B} = jAI_{tL} \]  \hspace{1cm} (B.13)

Now

\[ \bar{V}_{t} = V_{d} + jV_{q} = x_{q}I_{tLq} + j(eq' - x_{q}'I_{tLd}) \]  \hspace{1cm} (B.14)

\[ \bar{V}_{o} = cV_{DC}\cos\psi + jcV_{DC}\sin\psi \]  \hspace{1cm} (B.15)

\[ \bar{V}_{B} = V_{B}\sin\delta + jV_{B}\cos\delta \]  \hspace{1cm} (B.16)
\[ \tilde{I}_{tL} = I_{tLd} + jI_{tLq} \]  

(B.17)

Substituting all in B.13

\[
Z \left[ x_q I_{tLq} + j(eq' - x_d' I_{tLd}) \right] - \frac{X_{LB}}{X_{SDT}} (cV_{DC} \cos \psi + jcV_{DC} \sin \psi) \\
-(V_B \sin \delta + jV_B \cos \delta) = jA(I_{tLd} + jI_{tLq}) \\
\left[ Zx_q I_{tLq} - \frac{X_{LB}}{X_{SDT}} cV_{DC} \cos \psi - V_B \sin \delta \right] + j \left[ Z(eq' - x_d' I_{tLd}) \\
- \frac{X_{LB}}{X_{SDT}} cV_{DC} \sin \psi - V_B \cos \delta \right] = -AI_{tLq} + jAI_{tLd}
\]

Comparing the real and imaginary parts,

for real part

\[
Zx_q I_{tLq} - \frac{X_{LB}}{X_{SDT}} cV_{DC} \cos \psi - V_B \sin \delta = -AI_{tLq} \quad \text{(B.18)}
\]

\[
(Zx_q + A)I_{tLq} = \frac{X_{LB}}{X_{SDT}} cV_{DC} \cos \psi \quad \text{(B.19)}
\]

\[
I_{tLq} = \frac{X_{LB}}{X_{SDT}} cV_{DC} \cos \psi + V_B \sin \delta}{(Zx_q + A)} \quad \text{(B.20)}
\]

\[
I_{tLq} = \frac{X_{LB}}{X_{SDT}} cV_{DC} \cos \psi + V_B \sin \delta}{X_{tL} + X_{LB} + \frac{X_{LB}}{X_{SDT}} + \left( 1 + \frac{X_{LB}}{X_{SDT}} \right) x_q} \quad \text{(B.21)}
\]

Similarly from imaginary part

\[
Z(eq' - x_d' I_{tLd}) - \frac{X_{LB}}{X_{SDT}} cV_{DC} \sin \psi - V_B \cos \delta = AI_{tLd} \quad \text{(B.22)}
\]

\[
(A + Zx_d')I_{tLd} = Zeq' - \frac{X_{LB}}{X_{SDT}} cV_{DC} \sin \psi - V_B \cos \delta \quad \text{(B.23)}
\]
\[ I_{\text{Ld}} = \frac{Ze'q - \frac{X_{\text{LB}}}{X_{\text{SDT}}} cV_{\text{DC}} \sin \psi - V_B \cos \delta}{A + X_d'} \]  
(B.24)

\[ I_{\text{LLd}} = \frac{\left(1 + \frac{X_{\text{LB}}}{X_{\text{SDT}}} \right) eq' - \frac{X_{\text{LB}}}{X_{\text{SDT}}} cV_{\text{DC}} \sin \psi - V_B \cos \delta}{X_{\text{IL}} + X_{\text{LB}} + \frac{X_{\text{IL}}}{X_{\text{SDT}}} + \left(1 + \frac{X_{\text{LB}}}{X_{\text{SDT}}} \right) x_d'} \]  
(B.25)

Therefore the nonlinear model is given as:

\[ \dot{\delta} = \omega \omega \]  
(B.26)

\[ \dot{\omega} = \frac{1}{M} \left[ P_m - P_e - D \omega \right] \]  
(B.27)

\[ eq' = \frac{1}{T_d} \left[ E_{\text{fd}} - eq' - (x_d - x_d')I_{\text{Ld}} \right] \]  
(B.28)

\[ \dot{E}_{\text{fd}} = -\frac{1}{T_A} \left( E_{\text{fd}} - E_{\text{fdo}} \right) + \frac{K_A}{T_A} (V_{\text{io}} - V_t) \]  
(B.29)

\[ \dot{V}_{\text{dc}} = \frac{c}{C_{\text{DC}}} \left[ I_{\text{iod}} \cos \psi + I_{\text{ioq}} \sin \psi \right] \]  
(B.30)

where

\[ P_e = v_d I_{\text{Ld}} + v_q I_{\text{Lq}} \]

\[ = eq' I_{\text{Ld}} + (x_d - x_d') I_{\text{Ld}} I_{\text{Lq}} \]

\[ V_t = \sqrt{v_d^2 + v_q^2} = \sqrt{(eq' - x_d' I_{\text{Ld}})^2 + x_q'^2 I_{\text{Lq}}^2} \]

For Linear Model

\[ I_{\text{Ld}} = \frac{\left(1 + \frac{X_{\text{LB}}}{X_{\text{SDT}}} \right) eq' - \frac{X_{\text{LB}}}{X_{\text{SDT}}} cV_{\text{DC}} \sin \psi - V_B \cos \delta}{X_{\text{IL}} + X_{\text{LB}} + \frac{X_{\text{IL}}}{X_{\text{SDT}}} + \left(1 + \frac{X_{\text{LB}}}{X_{\text{SDT}}} \right) x_d'} \]  
(B.31)

\[ I_{\text{LLd}} = \frac{1}{A} \left[ Ze'q - \frac{X_{\text{LB}}}{X_{\text{SDT}}} cV_{\text{DC}} \sin \psi - V_B \cos \delta \right] \]  
(B.32)
where

\[
[A] = X_{IL} + X_{LB} + \frac{X_{IL}}{X_{SDT}} \left(1 + \frac{X_{LB}}{X_{SDT}}\right) x'_d
\]

\[Z = 1 + \frac{X_{LB}}{X_{SDT}}\]  \hspace{1cm} \text{(B.34)}

Linearizing

\[
\Delta I_{LD} = \frac{1}{[A]} \left[Z \Delta eq' - \frac{X_{LB}}{X_{SDT}} c_o V_{DCo} \cos \psi_o \Delta \psi - \frac{X_{LB}}{X_{SDT}} c_o \sin \psi_o \Delta V_{DC}\right. \\
\left. - \frac{X_{LB}}{X_{SDT}} V_{DCo} \sin \psi_o \Delta c + V_B \sin \delta_o \Delta \delta\right] \hspace{1cm} \text{(B.35)}
\]

\[
\Delta I_{LD} = \frac{Z}{[A]} \Delta eq' + \frac{V_B \sin \delta_o}{[A]} \Delta \delta + \left(-\frac{X_{LB}}{X_{SDT}[A]} V_{DCo} \sin \psi_o\right) \Delta c \times \\
\left(-\frac{X_{LB}}{X_{SDT}[A]} c_o V_{DCo} \cos \psi_o\right) \Delta \psi + \\
\left(-\frac{X_{LB}}{X_{SDT}[A]} c_o \sin \psi_o\right) \Delta V_{DC} \hspace{1cm} \text{(B.36)}
\]

\[
\Delta I_{LD} = C_5 \Delta eq' + C_6 \Delta \delta + C_7 \Delta \psi + C_8 \Delta c + C_9 \Delta V_{DC}\]  \hspace{1cm} \text{(B.37)}

Where

\[
C_5 = \frac{Z}{[A]}, \quad C_6 = \frac{V_B \sin \delta_o}{[A]}, \quad C_7 = -\frac{X_{LB} c_o V_{DCo} \cos \psi_o}{X_{SDT}[A]} \]

\[
C_8 = \frac{X_{LB} V_{DCo} \sin \psi_o}{X_{SDT}[A]}, \quad C_9 = -\frac{X_{LB} c_o \sin \psi_o}{X_{SDT}[A]} \]
Similarly

\[ I_{iLq} = \frac{V_B \sin \delta + \frac{X_{LB}}{X_{SDT}} cV_{DC} \cos \psi}{X_{tL} + X_{LB} + \frac{X_{LB}}{X_{SDT}} + \left(1 + \frac{X_{LB}}{X_{SDT}}\right) x_q} \quad (B.38) \]

\[ I_{iLq} = \frac{1}{[B]} \left[ V_B \sin \delta + \frac{X_{LB}}{X_{SDT}} cV_{DC} \cos \psi \right] \quad (B.39) \]

Linearizing

\[
\Delta I_{iLq} = \frac{1}{[B]} \left[ V_B \cos \delta_o \Delta \delta - \frac{X_{LB}}{X_{SDT}} c_o V_{DCo} \sin \psi_o \Delta \psi \\
+ \frac{X_{LB}}{X_{SDT}} c_o \sin \psi_o \Delta V_{DC} + \frac{X_{LB}}{X_{SDT}} V_{DCo} \sin \psi_o \Delta c_o \right] \quad (B.40)
\]

\[
\Delta I_{iLq} = \frac{V_B \cos \delta_o}{[B]} \Delta \delta + \left( -\frac{X_{LB}}{X_{SDT}[B]} c_o V_{DCo} \sin \psi_o \right) \Delta \psi \\
+ \left( \frac{X_{LB}}{X_{SDT}[A]} c_o V_{DCo} \cos \psi_o \right) \Delta c \\
+ \left( \frac{x_{LB}}{X_{SDT}[A]} c_o \cos \psi_o \right) \Delta V_{DC} \quad (B.41)
\]

\[
\Delta I_{iLq} = C_1 \Delta \delta + C_2 \Delta \psi + C_3 \Delta c + C_4 \Delta V_{DC} \quad (B.42)
\]

where

\[ C_1 = \frac{V_B \cos \delta_o}{[B]} , \quad C_2 = -\frac{X_{LB}}{X_{SDT}[B]} c_o V_{DCo} \sin \psi_o \]

\[ C_3 = \frac{X_{LB} V_{DCo} \cos \psi_o}{X_{SDT}[A]} , \quad C_4 = \frac{X_{LBCo} \cos \psi_o}{X_{SDT}[A]} \]
The linearized model of (B.27) to (B.30) is

\[ \Delta \dot{\delta} = \omega_b \Delta \omega \]  \hspace{1cm} (B.43)
\[ \Delta \dot{\omega} = -\frac{1}{M} \left[ \Delta P_e + D \Delta \omega \right] \]  \hspace{1cm} (B.44)
\[ \Delta e_q' = \frac{1}{T_{do}} \left[ -\Delta e_q' + \Delta E_{fd} \right] \]  \hspace{1cm} (B.45)
\[ \Delta \dot{E}_{fd} = -\frac{1}{T_A} \Delta E_{fd} - \frac{K_A}{T_A} \Delta V_i \]  \hspace{1cm} (B.46)
\[ \Delta V_{dc} = \frac{c}{C_{DC}} \left[ I_{iod} \cos \psi + I_{ioq} \sin \psi \right] \]  \hspace{1cm} (B.48)

Since

\[ e_q = e_q' + (x_d - x_d') I_{uid} \]

Therefore by linearizing

\[ \Delta e_q = \Delta e_q' + (x_d - x_d') \Delta I_{uid} \]

**Calculation of \( \Delta P_e \)**

\[ P_e = e_q' I_{tlq} + (x_q - x_q') I_{tlq} I_{tlq} \]  \hspace{1cm} (B.49)

linearizing

\[ \Delta P_e = e_q' \Delta I_{tlq} + I_{tlq} \Delta e_q' + (x_q - x_q') I_{tlq} \Delta I_{tlq} + (x_q - x_q') I_{tlq} \Delta I_{tlq} \]  \hspace{1cm} (B.50)

\[ = \left[ e_q' + (x_q - x_q') I_{tlq} \right] \Delta I_{tlq} + I_{tlq} \Delta e_q' + (x_q - x_q') I_{tlq} \Delta I_{tlq} \]  \hspace{1cm} (B.51)
Substituting the value of $\Delta I_{ldd}$ & $\Delta I_{lq}$

$$\Delta P_e = \left[ e q_o' + (x_q - x_d') I_{lqo} \right] \left\{ C_1 \delta + C_2 \Delta \psi + C_3 \Delta c + C_4 \Delta V_{DC} \right\} + I_{lqo} \Delta e q'$$

$$+ (x_q - x_d') I_{lqo} \left\{ C_5 \Delta \psi + C_6 \Delta \delta + C_7 \Delta \psi + C_8 \Delta c + C_9 \Delta V_{DC} \right\} \tag{B.52}$$

$$= \left\{ e q_o' + (x_q - x_d') I_{lqo} \right\} C_1 + \left\{ (x_q - x_d') I_{lqo} C_6 \right\} \Delta \delta + \left[I_{lqo} \left\{ 1 + (x_q - x_d') C_5 \right\} \right] \Delta e q'$$

$$+ \left[\left\{ e q_o' + (x_q - x_d') I_{lqo} \right\} C_4 + \left\{ (x_q - x_d') I_{lqo} C_9 \right\} \Delta V_{DC} \right.$$  

$$+ \left[ \left\{ e q_o' + (x_q - x_d') I_{lqo} \right\} C_3 + \left\{ (x_q - x_d') I_{lqo} C_8 \right\} \Delta c \right.$$  

$$+ \left[ \left\{ e q_o' + (x_q - x_d') I_{lqo} \right\} C_2 + \left\{ (x_q - x_d') I_{lqo} C_7 \right\} \Delta \psi \right. \tag{B.53}$$

Let

$$C_{111} = e q_o' + (x_q - x_d') I_{lqo}$$  

$$C_{112} = (x_q - x_d') I_{lqo}$$

Therefore

$$\Delta P_e = (C_{111} C_1 + C_{112} C_6) \Delta \delta + \left[I_{lqo} \left\{ 1 + (x_q - x_d') C_5 \right\} \right] \Delta e q'$$

$$+ (C_{111} C_4 + C_{112} C_9) \Delta V_{DC} + (C_{111} C_3 + C_{112} C_8) \Delta c$$

$$+ (C_{111} C_2 + C_{112} C_7) \Delta \psi \tag{B.54}$$

$$\Delta P_e = K_1 \delta + K_2 \Delta e q' + K_{pDC} \Delta V_{DC} + K_{pc} \Delta c + K_{p\psi} \Delta \psi \tag{B.55}$$

where

$$K_1 = C_{111} C_1 + C_{112} C_6,$$  

$$K_2 = I_{lqo} \left\{ 1 + (x_q - x_d') C_5 \right\}$$

$$K_{pDC} = C_{111} C_4 + C_{112} C_9,$$

$$K_{pc} = C_{111} C_3 + C_{112} C_8$$

$$K_{p\psi} = C_{111} C_2 + C_{112} C_7$$
Calculation of $\Delta eq$

\[
\Delta eq = \Delta eq' + (x_d - x_d')\Delta I_{ud}
\]

\[
= \Delta eq' + (x_d - x_d') \left( C_5 \Delta eq' + C_6 \Delta \delta + C_7 \Delta \psi + C_8 \Delta c + C_9 \Delta V_{DC} \right)
\]

\[
= \left\{ 1 + (x_d - x_d')C_5 \right\} \Delta eq' + (x_d - x_d')C_6 \Delta \delta + (x_d - x_d')C_7 \Delta \psi
\]

\[
+ (x_d - x_d')C_8 \Delta c + (x_d - x_d')C_9 \Delta V_{DC}
\]

Let

\[(x_d - x_d') = J \quad \text{(B.56)}\]

\[
\Delta eq = (1 + JC_5) \Delta eq' + JC_6 \Delta \delta + JC_7 \Delta \psi + JC_8 \Delta c + JC_9 \Delta V_{DC}
\]

\[
= K_3 \Delta eq' + K_4 \Delta \delta + K_{qq} \Delta \psi + K_{qc} \Delta c + K_{qDC} \Delta V_{DC}
\]

where

\[
K_3 = 1 + JC_5, \quad K_4 = JC_6, \quad K_{qq} = JC_7
\]

\[
K_{qc} = JC_8, \quad K_{qDC} = JC_9
\]

Calculation of $\Delta V_t$

\[
\Delta V_t = \frac{V_{gq}}{V_{to}} \Delta V_d + \frac{V_{go}}{V_{to}} \Delta V_q \quad \text{(B.57)}
\]

\[
= \frac{V_{gq}}{V_{to}} (x_q \Delta I_{Uq}) + \frac{V_{go}}{V_{to}} (\Delta eq' - x_d' \Delta I_{Ud}) \quad \text{(B.58)}
\]

\[
= \frac{V_{gq}}{V_{to}} (x_q C_5 \Delta eq' + C_6 \Delta \delta + C_7 \Delta \psi + C_8 \Delta c + C_9 \Delta V_{DC})
\]

\[
+ \frac{V_{go}}{V_{to}} (\Delta eq' - x_d' \Delta I_{Ud}) \quad \text{(B.59)}
\]
Let \( L = \frac{1}{\nu_{io}} \)

therefore

\[
\Delta V_t = L(V_{do}x_q C_1 - V_{qo}x'_d C_6) \Delta \delta + LV_{qo}(1 - x'_d C_5) \Delta eq' \\
+ L(V_{do}x_q C_4 - V_{qo}x'_d C_9) \Delta V_{DC} + L(V_{do}x_q C_3 - V_{qo}x'_d C_8) \Delta c \\
+ L(V_{do}x_q C_2 - V_{qo}x'_d C_7) \Delta \psi
\]  

(B.60)

\[
\Delta V_t = K_5 \Delta \delta + K_6 \Delta eq' + K_{VDC} \Delta V_{DC} + K_{Vc} \Delta c + K_{V\psi} \Delta \psi
\]  

(B.61)

where

\[
K_5 = L(V_{do}x_q C_1 - V_{qo}x'_d C_6), \\
K_6 = LV_{qo}(1 - x'_d C_5), \\
K_{V\psi} = L(V_{do}x_q C_2 - V_{qo}x'_d C_7), \\
K_{Vc} = L(V_{do}x_q C_3 - V_{qo}x'_d C_8), \\
K_{VDC} = L(V_{do}x_q C_4 - V_{qo}x'_d C_9)
\]

Substituting all values in the linearized model given by equations (B.44) to (B.48)

\[
\Delta \dot{\omega} = \omega_b \Delta \omega
\]  

(B.62)

\[
\Delta \omega = -\frac{1}{M} \left[ \{K_1 \Delta \delta + K_2 \Delta eq' + K_{pDC} \Delta V_{DC} + K_{pc} \Delta c + K_{p\psi} \Delta \psi\} + D \Delta \omega \right]
\]

\[
= -\frac{K_1}{M} \Delta \delta - \frac{K_2}{M} \Delta eq' - \frac{K_{pDC}}{M} \Delta V_{DC} - \frac{K_{pc}}{M} \Delta c - \frac{K_{p\psi}}{M} \Delta \psi - \frac{D}{M} \Delta \omega
\]

\[
= -\frac{K_1}{M} \Delta \delta - \frac{D}{M} \Delta \omega - \frac{K_2}{M} \Delta eq' - \frac{K_{pDC}}{M} \Delta V_{DC} - \frac{K_{pc}}{M} \Delta c - \frac{K_{p\psi}}{M} \Delta \psi
\]  

(B.63)
\[ \Delta e' = \frac{1}{T_{do'}} (-\Delta e + \Delta E_{fd}) \quad \text{(B.64)} \]

\[ \Delta e'' = \frac{1}{T_{do'}} \left[ -(K_5 \Delta e' + K_4 \Delta \delta + K_{q'\psi} \Delta \psi + K_{q'c} \Delta c + K_{q'DC} \Delta V_{DC}) + \Delta E_{fd} \right] \]

\[ = \frac{K_4}{T_{do'}} \Delta \delta - \frac{K_5}{T_{do'}} \Delta e' + \frac{1}{T_{do'}} \Delta E_{fd} - \frac{K_{q'DC}}{T_{do'}} \Delta V_{DC} - \frac{k_{qc}}{T_{do'}} \Delta c \]

\[ - \frac{F_{q'\psi}}{T_{do'}} \Delta \psi \quad \text{(B.65)} \]

\[ \Delta E_{fd} = -\frac{1}{T_A} \Delta E_{fd} - \frac{K_A}{T_A} \Delta V_i \quad \text{(B.66)} \]

\[ = -\frac{1}{T_A} \Delta E_{fd} - \frac{K_A}{T_A} \]

\[ [K_5 \Delta \delta + K_6 \Delta e' + K_{VDC} \Delta V_{DC} + k_{Vc} \Delta c + K_{V'\psi} \Delta \psi] \quad \text{(B.67)} \]

\[ = -\frac{K_A k_5}{T_A} \Delta \delta - \frac{K_A K_6}{T_A} \Delta e' - \frac{1}{T_A} \Delta E_{fd} - \frac{K_A k_{VDC}}{T_A} \Delta V_{DC} \]

\[ - \frac{K_{Vc} K_A}{T_A} \Delta c - \frac{K_{V'\psi} K_A}{T_A} \Delta \psi \quad \text{(B.68)} \]
In Matrix form

\[
\begin{bmatrix}
\Delta \delta \\
\Delta \omega \\
\Delta \dot{\psi}
\end{bmatrix}
= \begin{bmatrix}
0 & \omega_b & 0 & 0 \\
-K_1/M & -D/M & -K_2/M & 0 \\
-K_4/T_{d\sigma} & 0 & -K_3/T_{d\sigma} & 1/T_{d\sigma} \\
-k_A K_5/T_A & 0 & -K_A K_6/T_A & -1/T_A
\end{bmatrix}
\begin{bmatrix}
\Delta \delta \\
\Delta \omega \\
\Delta \psi
\end{bmatrix} +
\begin{bmatrix}
0 \\
-K_{pDC}/M \\
-K_{qDC}/T_{d\sigma} \\
-k_A K_{VDC}/T_A
\end{bmatrix}
\Delta V_{DC} +
\begin{bmatrix}
0 & 0 \\
-K_{pc}/M & -K_{p\psi}/M \\
-K_{qc}/T_{d\sigma} & -K_{q\psi}/T_{d\sigma} \\
-k_A K_{Vc}/T_A & -K_A K_{V\psi}/T_A
\end{bmatrix}
\begin{bmatrix}
\Delta c \\
\Delta \psi
\end{bmatrix} \tag{B.69}
\]

Now,

\[
\tilde{I}_{Lo} = \frac{V_L - V_0}{j X_{SDT}} \tag{B.70}
\]

\[
\tilde{I}_{Lo} = \frac{V_{i} - j X_{L} I_{L} - V_0}{j X_{SDT}} \tag{B.71}
\]
Substituting values of $I_{loq}, \tilde{V}_t, I_{Lq}, \tilde{V}_0$

\[
I_{loq} + j\tilde{I}_{loq} = \frac{1}{jX_{SDT}}[X_q I_{Lq} + j(eq' - X_d' I_{Lq}) - j X_{Lq} (I_{Lq} + j I_{Lq}) - c V_{DC}(\cos \psi + j \sin \psi)] \tag{B.72}
\]

\[
I_{loq} + j\tilde{I}_{loq} = \frac{1}{jX_{SDT}}[x_q I_{Lq} + j(eq' - x_d' I_{Lq}) - j X_{Lq} I_{Lq} - X_{Lq} \tilde{I}_{Lq} - c V_{DC} \cos \psi - j c V_{DC} \sin \psi] \tag{B.73}
\]

\[
I_{loq} + j\tilde{I}_{loq} = \frac{1}{jX_{SDT}}[(x_q + x_{Lq}) I_{Lq} - c V_{DC} \cos \psi] + j [eq' - (x_d' + x_{Lq}) I_{Lq} - c V_{DC} \sin \psi] \tag{B.74}
\]

\[
I_{loq} + j\tilde{I}_{loq} = \frac{eq' - (x_d' + x_{Lq}) I_{Lq} - c V_{DC} \sin \psi}{X_{SDT}} + \frac{\{c V_{DC} \cos \psi - (x_d' + x_{Lq}) I_{Lq}\}}{X_{SDT}} \tag{B.75}
\]

Comparing real & Imaginary Parts

\[
\bar{I}_{loq} = \frac{eq'}{X_{SDT}} - \frac{(x_d' + x_{Lq}) I_{Lq}}{X_{SDT}} - \frac{c V_{DC} \sin \psi}{X_{SDT}} \tag{B.76}
\]

\[
\bar{I}_{loq} = \frac{\{c V_{DC} \cos \psi - (x_d' + x_{Lq}) I_{Lq}\}}{X_{SDT}} - \frac{(x_q + x_{Lq}) I_{Lq}}{X_{SDT}} \tag{B.77}
\]

linearizing equation B.76 and B.77

\[
\Delta \bar{I}_{loq} = \frac{1}{x_{SDT}} \Delta eq' - \frac{\{x_d' + x_{Lq}\}}{X_{SDT}} \Delta \bar{I}_{Lq} - \frac{c_0 V_{DC} \cos \psi_0 \Delta \psi - c_0 \sin \psi_0 \Delta V_{DC}}{X_{SDT}} \tag{B.78}
\]

\[
\Delta \bar{I}_{loq} = \frac{1}{X_{SDT}} \Delta eq' - \frac{\{x_d' + x_{Lq}\}}{X_{SDT}} \{c_0 \Delta eq' + C_0 \Delta \delta + C_7 \Delta \psi + C_8 \Delta c + \}

\]

\[
C_9 \Delta V_{DC} \cos \psi_0 \Delta \psi - \frac{c_0 \sin \psi_0 \Delta V_{DC}}{X_{SDT}} - \frac{V_{DC} \sin \psi_0 \Delta \psi}{X_{SDT}} \tag{B.79}
\]

\[
\Delta \bar{I}_{loq} = \frac{1}{x_{SDT}} (1 - (x_d' + X_{Lq}) C_0) \Delta eq' - \frac{(x_d' + X_{Lq}) C_0 \Delta \delta - \{x_d' + X_{Lq}\} C_7 \Delta \psi - \}

\]

\[
\frac{(x_d' + X_{Lq}) C_8 \Delta c}{X_{SDT}} - \frac{(x_d' + X_{Lq}) C_9 \Delta V_{DC} - c_0 V_{DC} \cos \psi_0 \Delta \psi - \}

\]

\[
\frac{c_0 \sin \psi_0 \Delta V_{DC}}{X_{SDT}} - \frac{V_{DC} \sin \psi_0 \Delta \psi}{X_{SDT}} \tag{B.80}
\]
Let
\[ \frac{x_d' + X_{IL}}{X_{SDT}} = E \quad \text{and} \quad \frac{\sin \psi_o}{X_{SDT}} = G \]

\[ \Delta I_{lod} = \frac{1}{X_{SDT}} \{1 - (x_d' + X_{IL}C_3)\} \Delta e q' - EC_6 \Delta \delta - EC_7 \Delta \psi - EC_8 \Delta c \]

\[ -EC_9 \Delta V_{DC} - \frac{c_o V_{DCo \cos \psi_o}}{X_{SDT}} \Delta \psi - GC_o \Delta V_{DC} - GV_{DCo} \Delta c \]  \( \text{(B.81)} \)

\[ \Delta I_{lod} = C_{10} \Delta e q' + C_{11} \Delta \delta + C_{12} \Delta \psi + C_{13} \Delta c + C_{14} \Delta V_{DC} \]  \( \text{(B.82)} \)

where \( C_{10} = \frac{1}{X_{SDT}} \{1 - (x_d' + X_{IL}C_3)\} \), \( C_{11} = -EC_6 \)

\( C_{12} = -\{EC_7 + \frac{c_o V_{DCo \cos \psi_o}}{X_{SDT}}\} \), \( C_{13} = -\{EC_8 + GV_{DCo}\} \)

\( C_{14} = -\{EC_9 + GC_o\} \)

Similarly

\[ \Delta I_{lq} = -\frac{c_o V_{DCo \sin \psi_o}}{X_{SDT}} \Delta \psi + \frac{c_o \cos \psi_o}{X_{SDT}} \Delta V_{DC} + \frac{V_{DCo \cos \psi_o}}{X_{SDT}} \Delta c \]

\[ -\frac{(x_q + x_{IL})}{X_{SDT}} \Delta I_{lLq} \]  \( \text{(B.83)} \)

\[ \Delta I_{lq} = -\frac{c_o V_{DCo \sin \psi_o}}{X_{SDT}} \Delta \psi + \frac{c_o \cos \psi_o}{X_{SDT}} \Delta V_{DC} + \frac{V_{DCo \cos \psi_o}}{X_{SDT}} \Delta c - \]

\[ \frac{(x_q + X_{IL})}{X_{SDT}} \{C_1 \Delta \delta + C_2 \Delta \psi + C_3 \Delta c + C_4 \Delta V_{DC}\} \]  \( \text{(B.84)} \)

\[ \Delta I_{lq} = -\frac{(x_q + X_{IL})}{X_{SDT}} C_1 \Delta \delta - \{c_o V_{DCo \sin \psi_o} + (\frac{x_q + X_{IL}}{X_{SDT}})C_2\} \Delta \psi + \]

\[ \left\{ \frac{c_o \cos \psi_o}{X_{SDT}} - \frac{(x_q + X_{IL})}{X_{SDT}} \right\} \Delta V_{DC} + \]

\[ \left\{ \frac{V_{DCo \cos \psi_o}}{X_{SDT}} + \frac{(x_q + X_{IL})}{X_{SDT}} C_3 \right\} \Delta c \]  \( \text{(B.85)} \)

Let

\[ \frac{(x_q + X_{IL})}{X_{SDT}} = W \]
\[ \Delta I_{loq} = -WC_1 \Delta \delta - \{ c_o V_{DCo} G + WC_2 \} \Delta \psi + \{ \frac{c_o\cos\psi_o}{X_{SDT}} - WC_4 \} \Delta V_{DC} + \{ \frac{V_{DCo}\cos\psi_o}{X_{SDT}} - WC_3 \} \Delta c \] (B.86)

\[ \Delta I_{loq} = C_{15} \Delta \delta + C_{16} \Delta \psi + C_{17} \Delta V_{DC} + C_{18} \Delta c \] (B.87)

where \( C_{15} = -WC_1 \), \( C_{16} = -\{ c_o V_{DCo} G + WC_2 \} \)

\[ C_{17} = \left\{ \frac{c_o\cos\psi_o}{X_{SDT}} - WC_4 \right\}, \quad C_{18} = \left\{ \frac{V_{DCo}\cos\psi_o}{X_{SDT}} - WC_3 \right\} \]

Now since the expression for \( V_{DC} \) is given as

\[ V_{DC} = \frac{c}{C_{DC}} (I_{loq}\cos\psi + I_{loq}\sin\psi) \] (B.88)

linearizing with \( \frac{1}{C_{DC}} = N \)

\[ \Delta V_{DC} = N[(I_{loq}\cos\psi_o + I_{loq}\sin\psi_0)\Delta c + c_o(-I_{loq}\sin\psi_o + I_{loq}\cos\psi_o)\Delta \psi + c_o (\cos\psi_o \Delta I_{loq} + \sin\psi_o \Delta I_{loq})] \] (B.89)

Substituting the value of \( \Delta I_{loq} \) and \( \Delta I_{loq} \)

\[ \Delta V'_{DC} = N[(I_{loq}\cos\psi_o + I_{loq}\sin\psi_o)\Delta c + c_o(-I_{loq}\sin\psi_o + I_{loq}\cos\psi_o)\Delta \psi + c_o \{ \cos\psi_o (C_{10} \Delta e_{eq'} + C_{11} \Delta \delta + C_{12} \Delta \psi + C_{13} \Delta c + C_{14} \Delta V_{DC}) + \sin\psi_o (C_{15} \Delta \delta + C_{16} \Delta \psi + C_{17} \Delta V_{DC} + C_{18} \Delta c) \}] \] (B.90)

\[ \Delta V''_{DC} = Nc_o (\cos\psi_o C_{14} + \sin\psi_o C_{15}) \Delta \delta + (Nc_o \cos\psi_o C_{10}) \Delta e_{eq'} + Nc_o (\cos\psi_o C_{14} + \sin\psi_o C_{17}) \Delta V_{DC} + N(I_{loq} \cos\psi_o + I_{loq} \sin\psi_o C_{13} + c_o \sin\psi_o C_{18}) \Delta c + Nc_o (-I_{loq} \sin\psi_o + I_{loq} \cos\psi_o + c_o \cos\psi_o C_{12} + \sin\psi_o C_{16}) \Delta \psi \] (B.91)

\[ \Delta V_{DC} = K_7 \Delta \delta + K_8 \Delta e_{eq'} + k_9 \Delta V_{DC} + K_{DC} \Delta c + K_{d\psi} \Delta \psi \] (B.92)
where

\[ K_7 = N_0 c (\cos \psi_o C_{11} + \sin \psi_o C_{15}) \]
\[ K_8 = N_0 c \cos \psi_o C_{10} \]
\[ K_9 = N_0 c (\cos \psi_o C_{14} + \sin \psi_o C_{17}) \]
\[ K_{DC} = N(I_{lod} \cos \psi_o + I_{lqdo} \sin \psi_o + c \cos \psi_o C_{13} + c \sin \psi_o C_{18}) \]
\[ k_{d\psi} = N_0 c (-I_{lod} \sin \psi_o + I_{lqdo} \cos \psi_o + \cos \psi_o C_{12} + \sin \psi_o C_{16}) \]

In Matrix form

\[
\begin{bmatrix}
\Delta \delta \\
\Delta \omega \\
\Delta e_{q'} \\
\Delta \dot{E}_{fd} \\
\Delta \dot{V}_{DC}
\end{bmatrix}
= \begin{bmatrix}
0 & \omega_o & 0 & 0 & 0 \\
-K_1/M & -D/M & -K_1/M' & 0 & -K_{pDC}/M \\
-K_4/T_{d'} & 0 & -K_4/T_{d'} & 1/T_{d'} & -K_{4DC}/T_{d'} \\
-K_A K_5/T_A & 0 & -K_A K_5/T_A & -1/T_A & -K_A K_{VDC}/T_A \\
K_7 & 0 & K_8 0 & K_9 & 0
\end{bmatrix}
\begin{bmatrix}
\Delta \delta \\
\Delta \omega \\
\Delta e' \\
\Delta E_{fd} \\
\Delta V_{DC}
\end{bmatrix}
+ \begin{bmatrix}
\Delta c \\
\Delta \psi
\end{bmatrix}
\]

(B.93)
Appendix C

STATCOM and Controller Data

- Parameters for the approximate model (in p.u. except indicated)

\[ H = 3s, \quad D = 4.0, \quad K = 1.0, \quad x_1 = 0.3, \quad x_2 = 0.3, \quad x_d' = 0.3, \quad x_d = 1.0, \quad T = 0.02, \]
\[ I_{so} = 0. \]

- Parameters for the Detailed model (in p.u. except indicated)

\[ H = 3s, \quad T_{do}' = 6.3, \quad x_d = 1.0, x_d' = 0.3, \quad x_q = 0.6. \quad D = 4.0, \quad x_{TL} = 0.3, \]
\[ x_{LB} = 0.3, \quad x_{SST} = 0.15, \quad K_A = 10.0, T_A = 0.01s, \quad T_C = 0.05s, \quad C_{DC} = 1.0, \]
\[ c_o = 0.25, \quad \psi_o = 46.52^\circ \]

- Nominal Plant Operating condition:

\[ P_{eo} = 0.9, V_{to} = 1.0, p.f. = 1.0 \]
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